



**AGH UNIVERSITY OF SCIENCE
AND TECHNOLOGY**

AGH Krakow, Poland



Mössbauer Spectroscopy of Fe-Cr Alloys

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Stainless steels

- Must contain $\geq 10.5\%$ Cr and low content of carbon



Harry Brearley



Albert Portevin



H. Goldsmidt



M. Mauermann

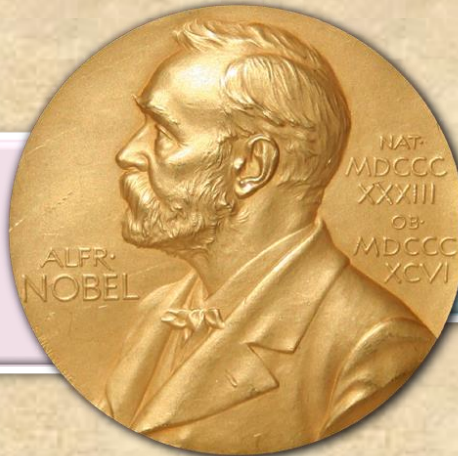
- Discovered in 1900 – 1915 as effort of investigations of many people; Leon Guillet (F), Giesen (GB), Harry Brearley(GB), Hans Goldsmidt (D), Albert Portevin (F), Borchers (D) and Max Mauermann (PL)

Mössbauer Spectroscopy in Fe-Cr Alloys

Two aspects

Industrio-
technological

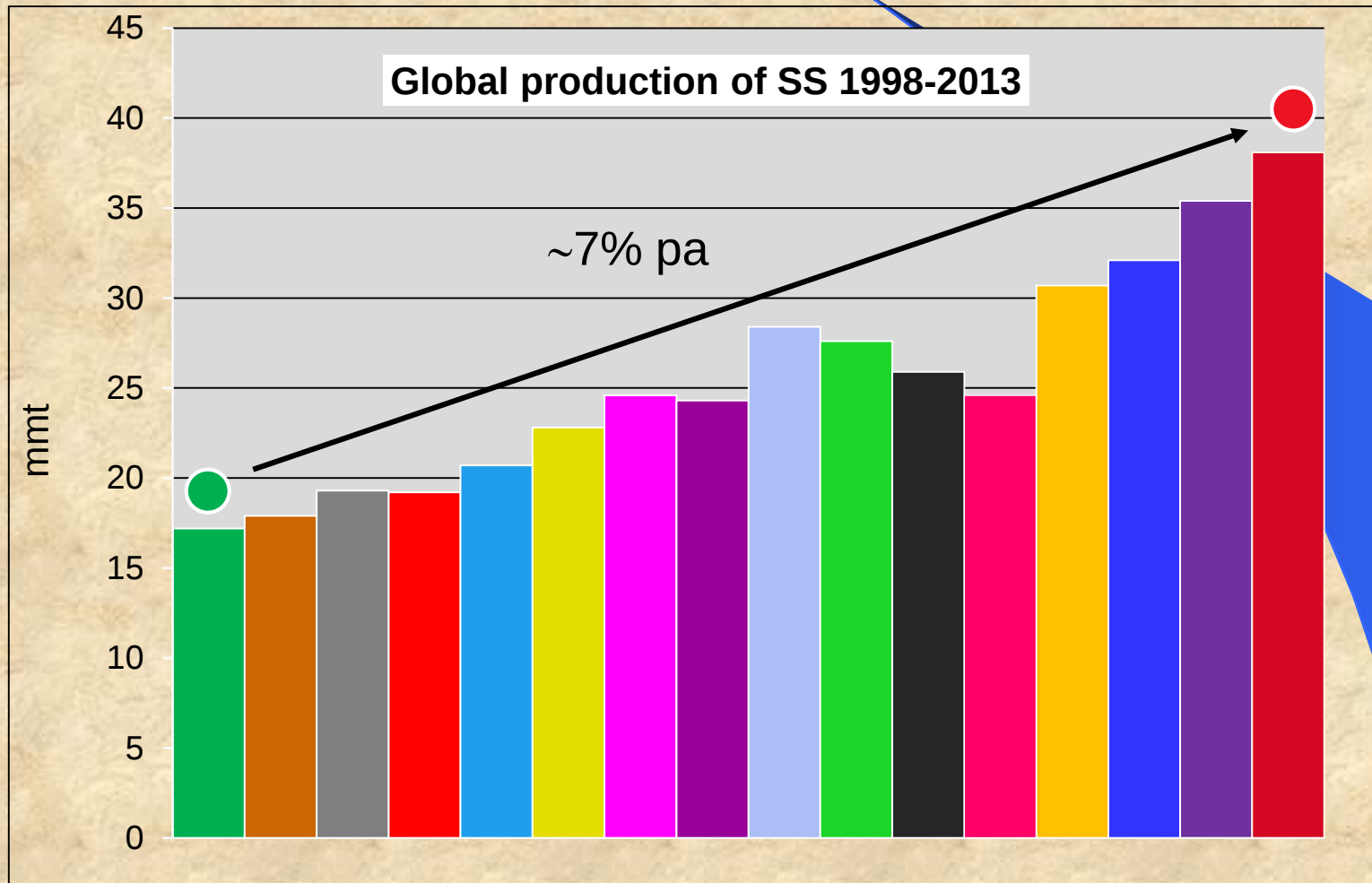
2007
For GMR



Scientific

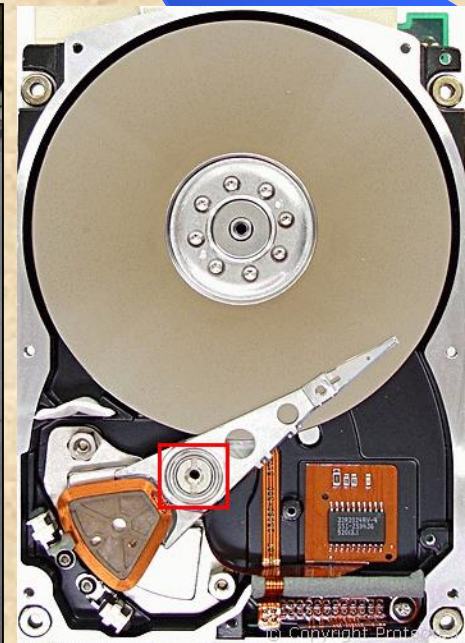
Mössbauer Spectroscopy in Fe-Cr Alloys

- Aspect industrio-technological •



Mössbauer Spectroscopy in Fe-Cr Alloys

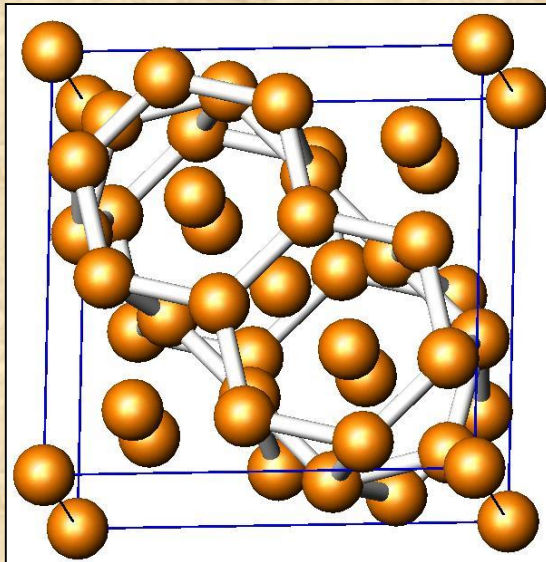
- Industrio-technological aspect •



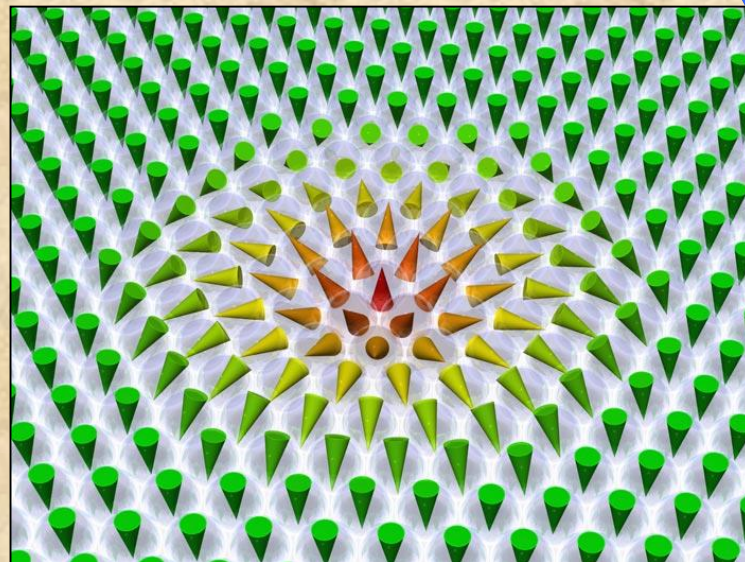
Mössbauer Spectroscopy in Fe-Cr Alloys

- Scientific aspect •

Crystallographic



Magnetic



MS in Fe-Cr Alloys

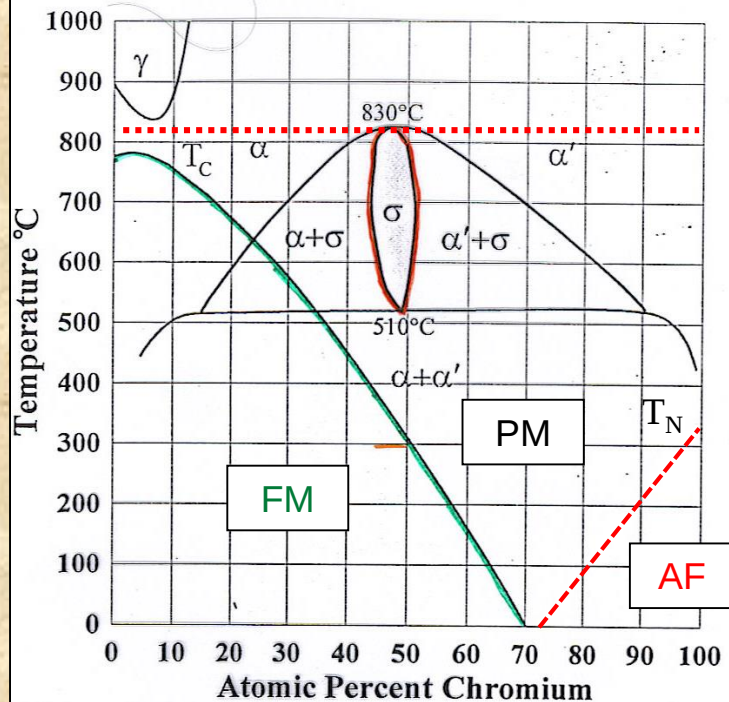
• Crystallographic •

◆ Different phases: α , α' , γ , σ

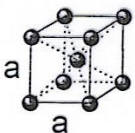
◆ Phase transitions: $\alpha \leftrightarrow \gamma$, $\alpha \leftrightarrow \sigma$

◆ Phase decomposition: α , α'

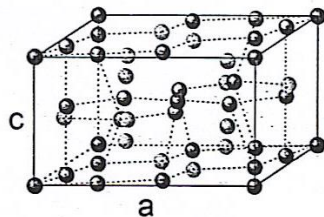
Phase diagram of Fe-Cr



α



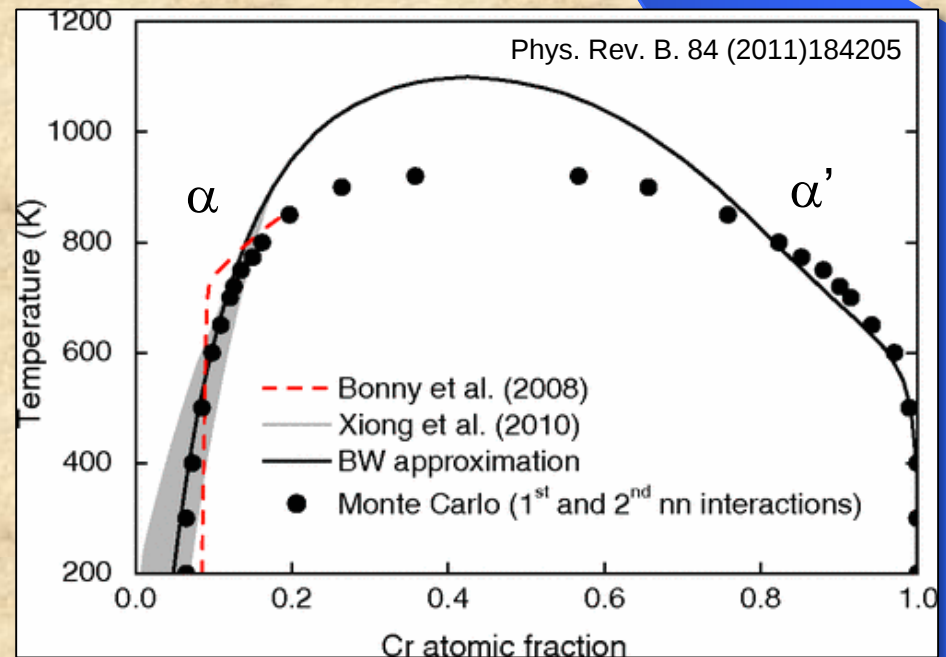
σ



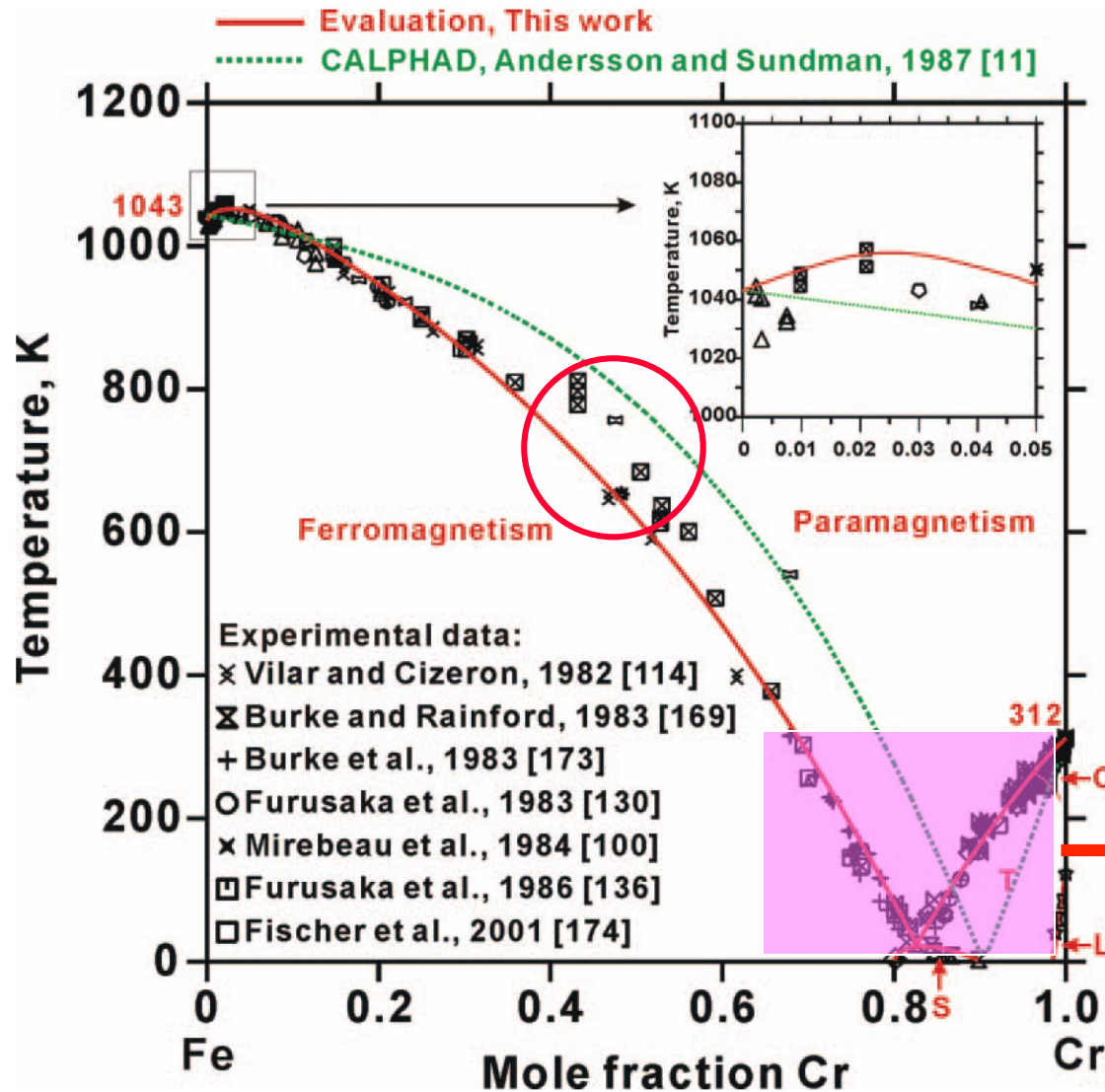
$$a = 2.877 \text{ \AA}$$

$$a = 8.797 \text{ \AA}$$

$$c = 4.558 \text{ \AA}$$



Mössbauer Spectroscopy in Fe-Cr Alloys



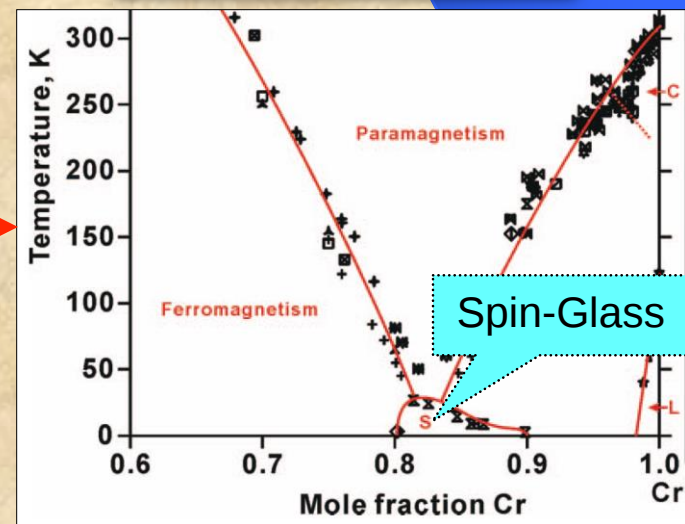
• Magnetic •

◆ Ferromagnetism

◆ Antiferromagnetism

◆ Spin-glass

◆ Re-entrance

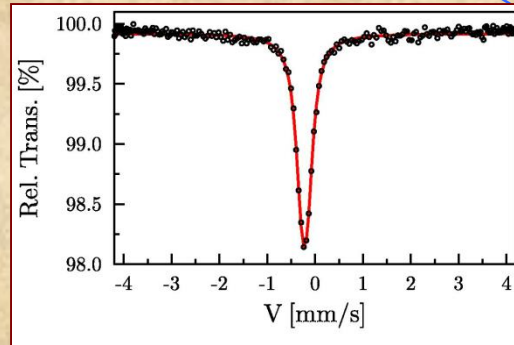


Mössbauer Spectroscopy is one of the most relevant techniques to study Fe-Cr Alloys

- Spin- and charge-density changes
- Identification of α , γ and σ phases
- Kinetics of phase formation e. g. $\alpha \rightarrow \sigma$
- Short-range ordering (SRO)
- Phase decomposition (α , α')
- Curie temperature
- Néel temperature
- Spin-glass freezing temperature
- Re-entrance transition
- Corrosion
- Texture

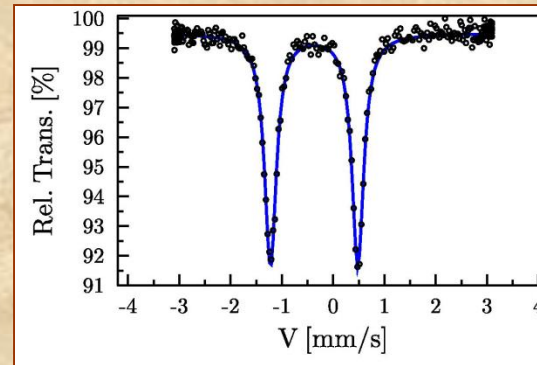
MS and Hyperfine Interactions

$\mathcal{E}0$

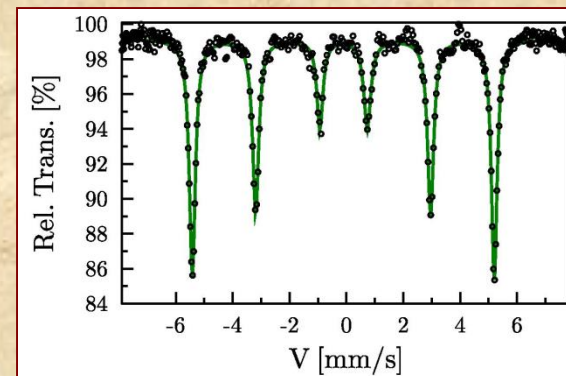
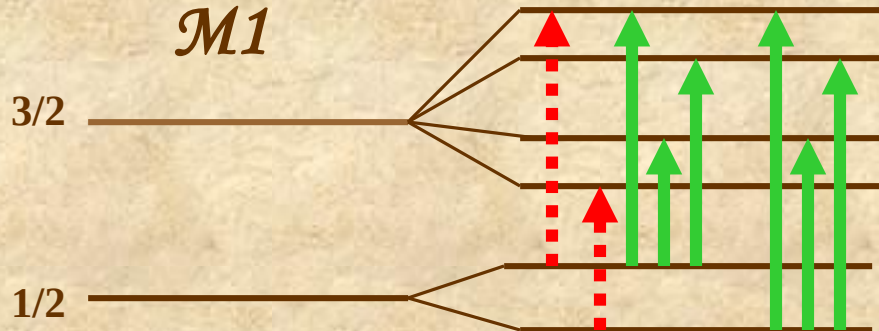


$$\mathcal{H} = \mathcal{E}0 + \mathcal{E}2 + \mathcal{M}1$$

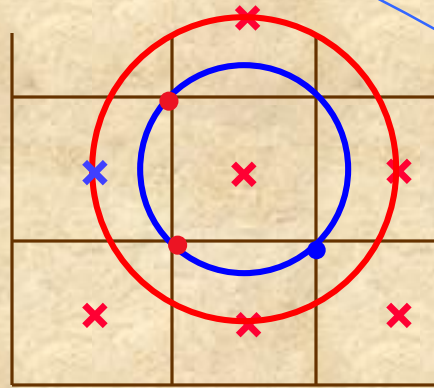
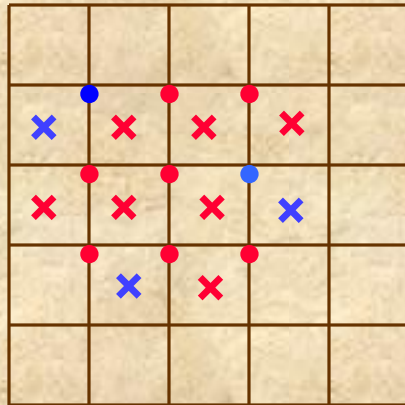
$\mathcal{E}2$



$\mathcal{M}1$



Spin- and charge-density

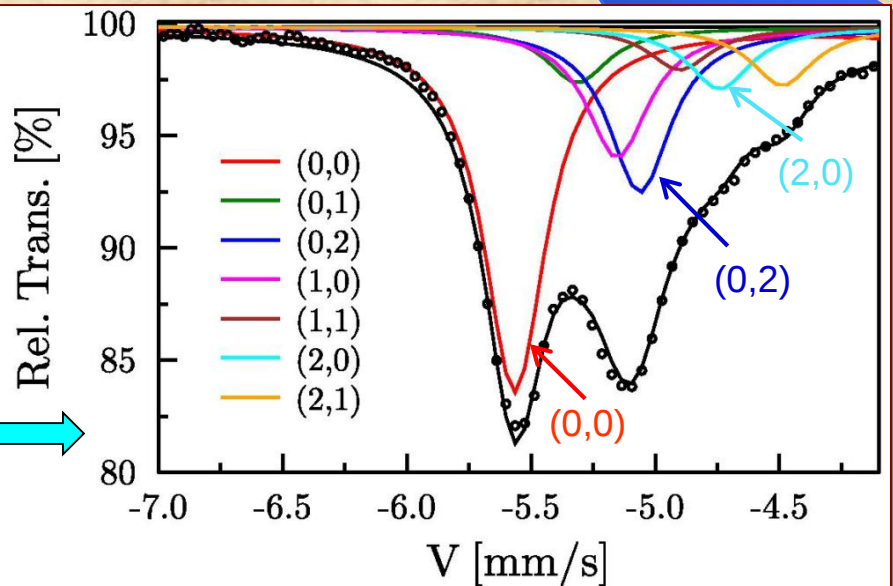
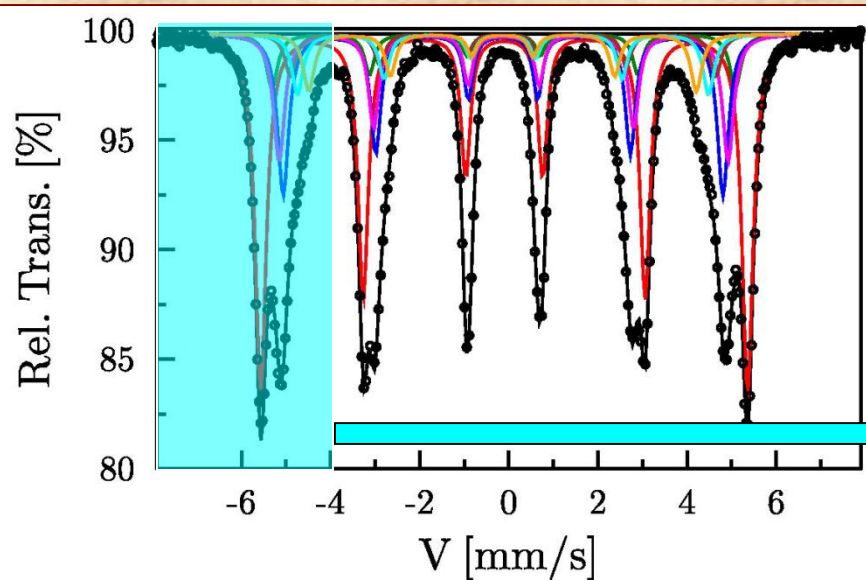


(1,1)

bcc: 1NN=8, 2NN=6

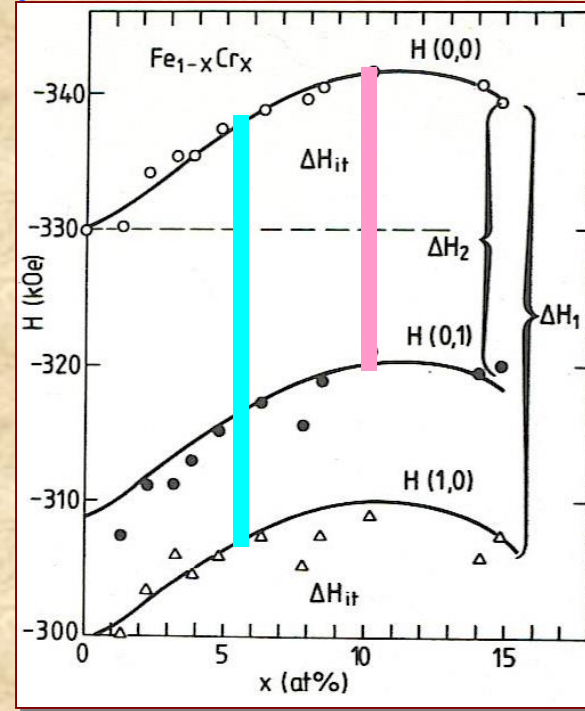
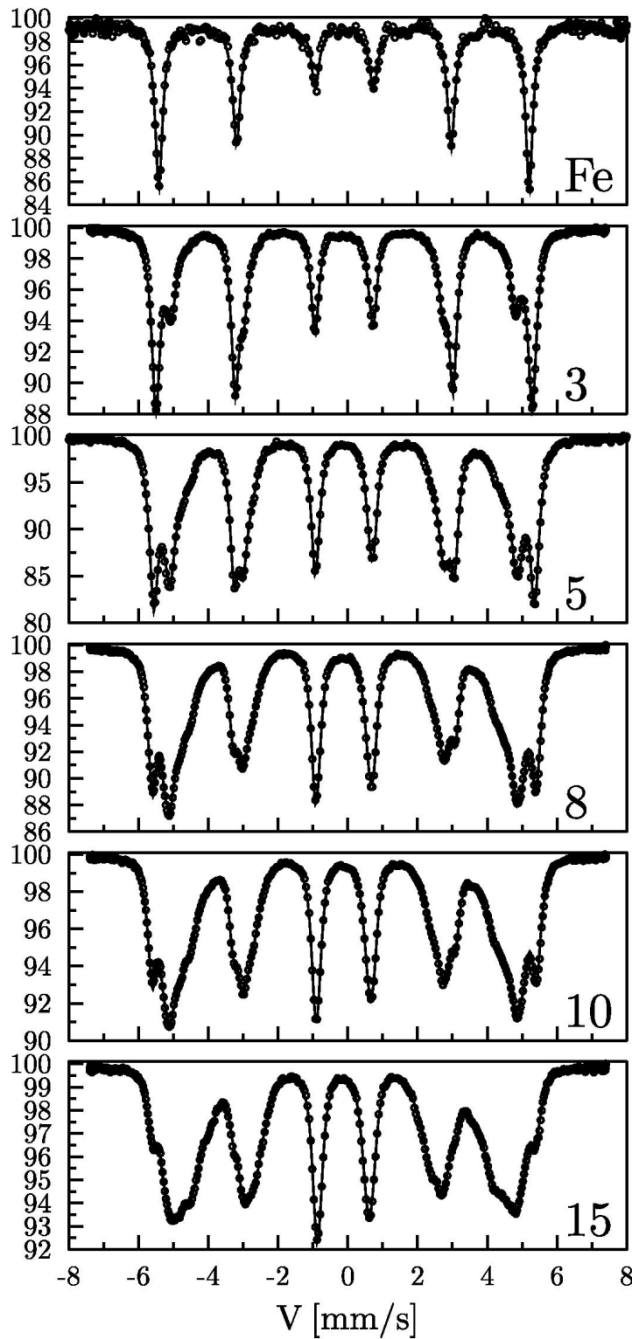
$$P_r(m, n; x) = \binom{8}{m} \binom{6}{n} x^{m+n} (1-x)^{14-m-n}$$

x = 5 at% Cr



Spin & charge

Rel. Transmission [%]



$$\Delta H_1 = 3.2T$$

$$\Delta H_2 = 2.2T$$

$$H(m,n:x) = H(0,0:x) - m\Delta H_1 - n\Delta H_2$$

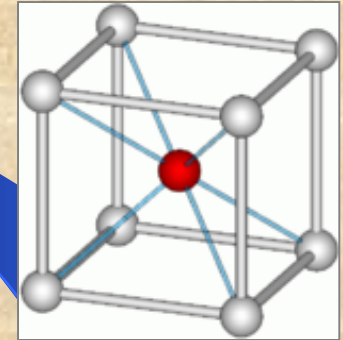
Spin- & charge-density changes

- Local charge-density changes on Fe sites:

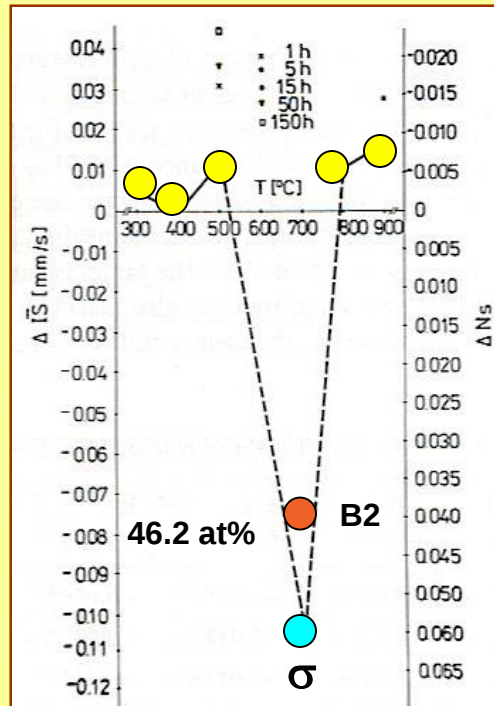
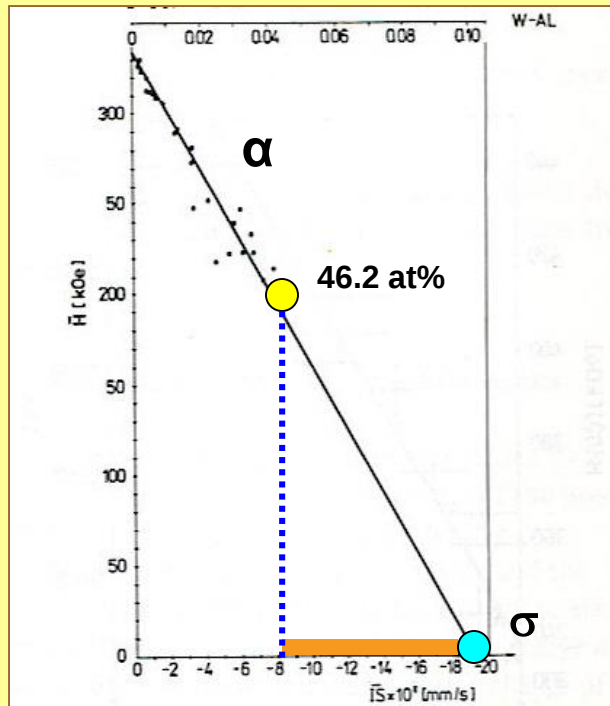
1NN: $\Delta I_1 = -0.023 \text{ mm/s} = 0.012 \text{ s-electron/Cr atom}$

2NN: $\Delta I_2 = -0.007 \text{ mm/s} = 0.007 \text{ s-electron/Cr atom}$

$$q_{\max}^{\alpha} \approx 0.04 e$$



- Average changes:



$$\frac{\Delta H_1}{\Delta H_2} \approx \frac{\Delta I_1}{\Delta I_2} \approx 1.5$$



Electrons with spin-up
flow from Cr to Fe

$$\Delta I = I_{\sigma} - I_{\alpha} = -0.11 \text{ mm/s} \approx 0.06 e$$

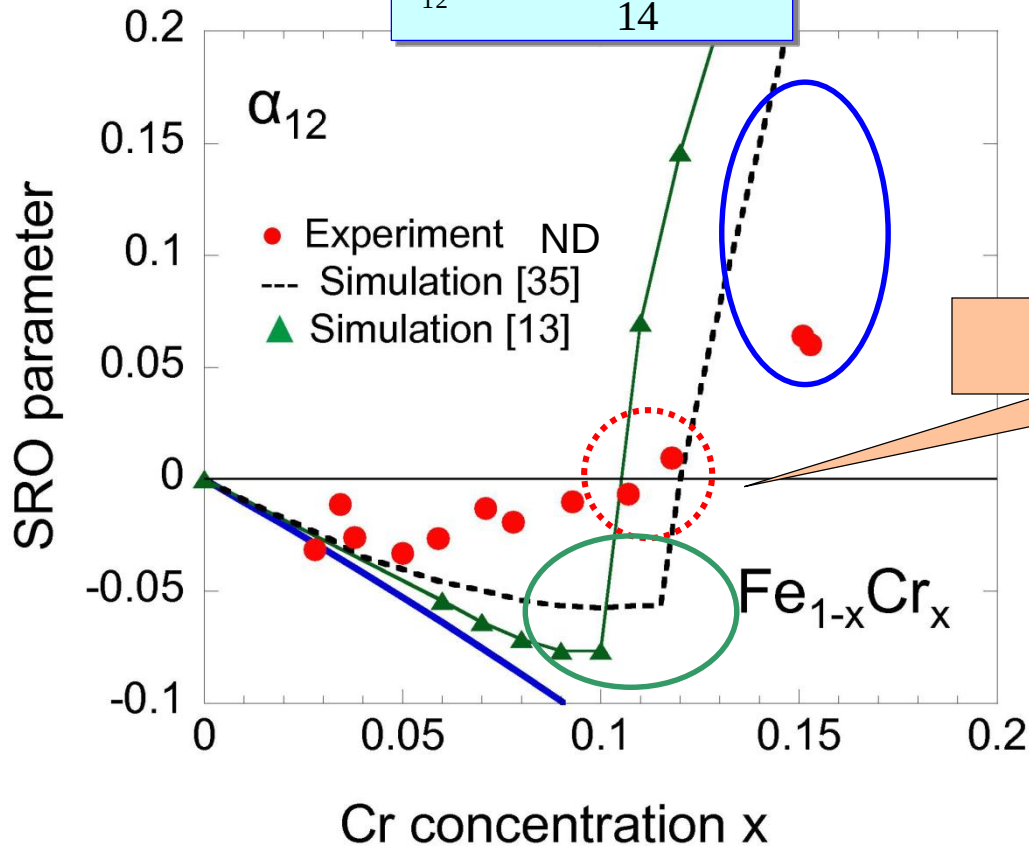
SRO in Fe-Cr

- Cowley SRO parameter, α_n :

I. Mirebeau, G. Parette Phys. Rev. B, 82 (2010) 104203)

$p_{FeCr}(n)$ – probability of finding one Cr atom in the n -th shell around a Fe atom

$$\alpha_{12} = \frac{8\alpha(1,0) + 6\alpha(0,1)}{14}$$



$$\alpha_n = 1 - \frac{p_{FeCr}(n)}{x} \quad (1)$$

INVERSION

SRO in Fe-Cr - MS

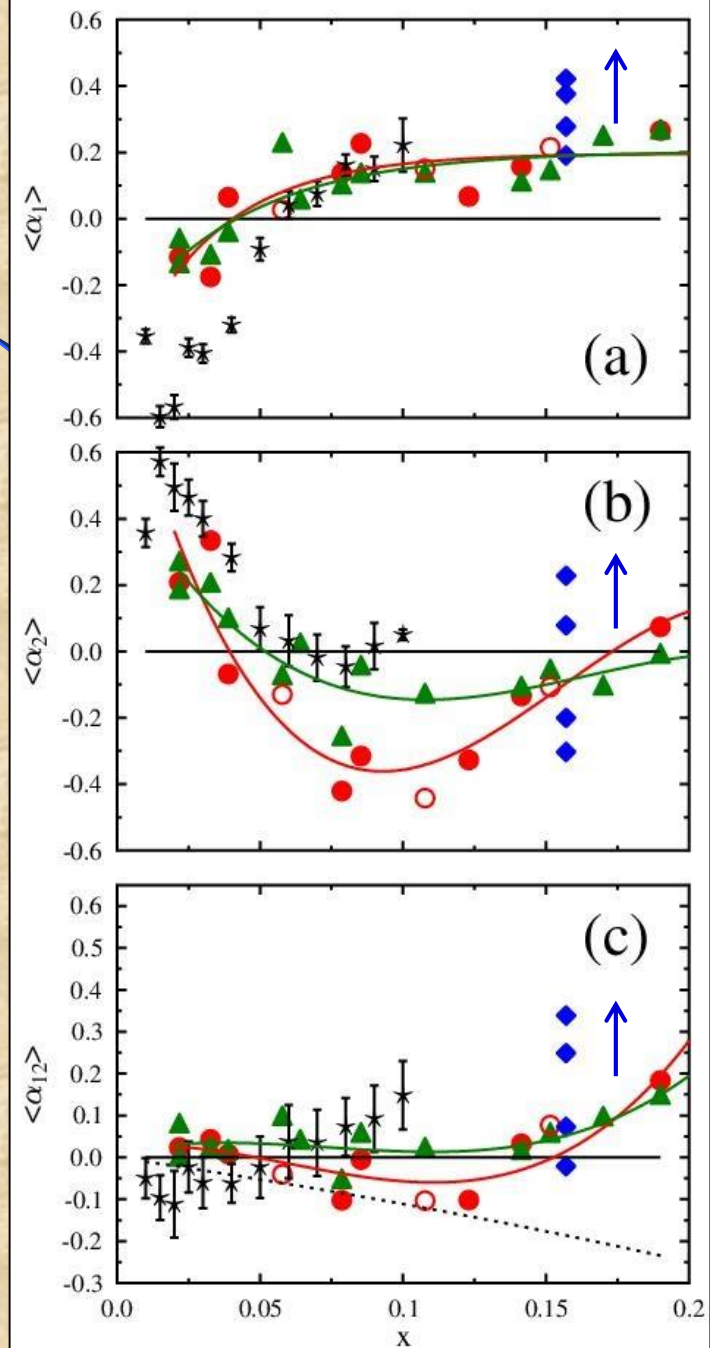
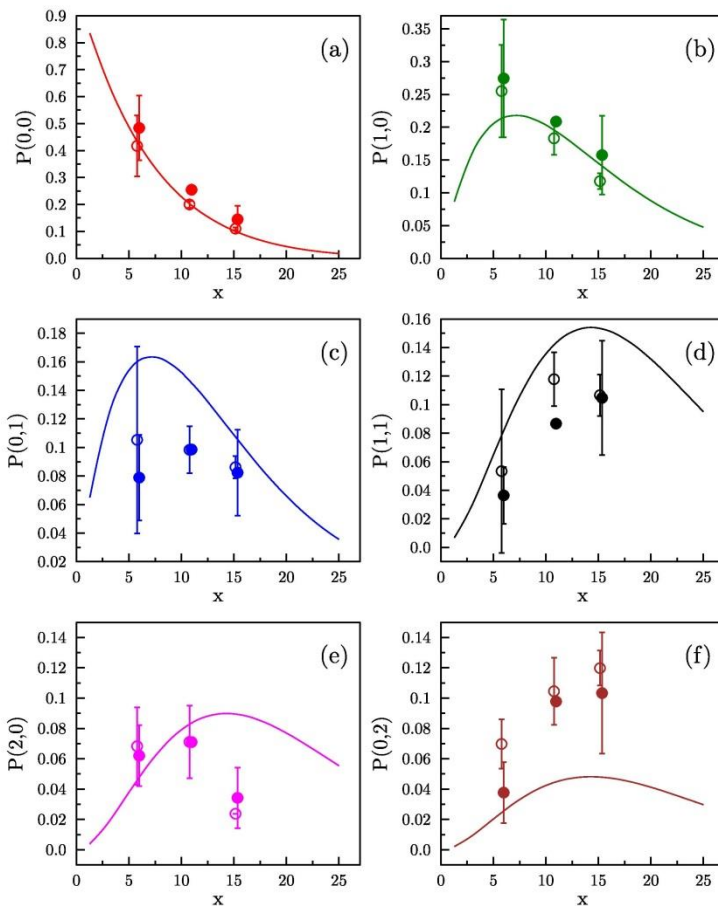
O - cold rolled

● - quenched

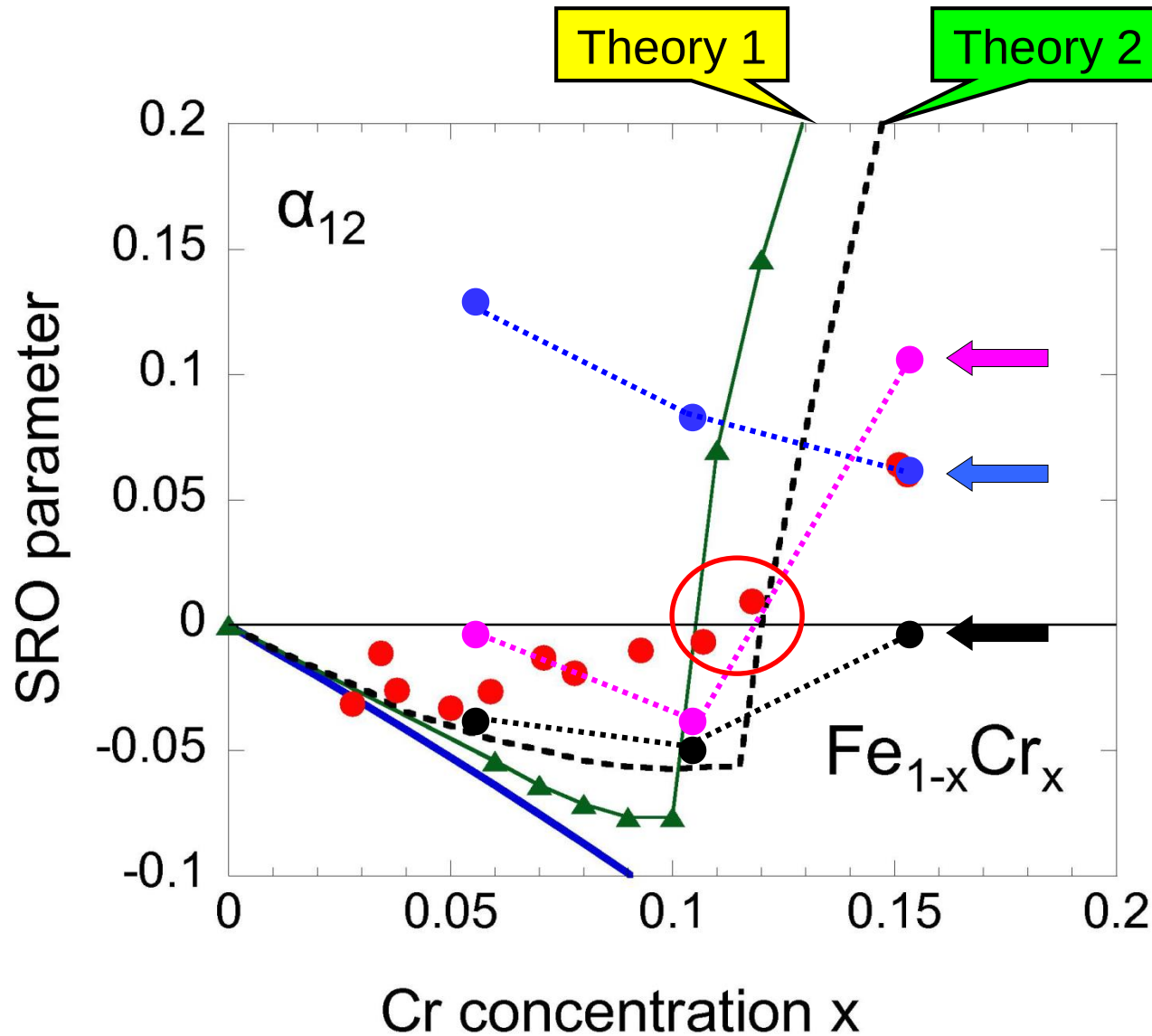
▲ - Q

● - EQ

◆ - IA

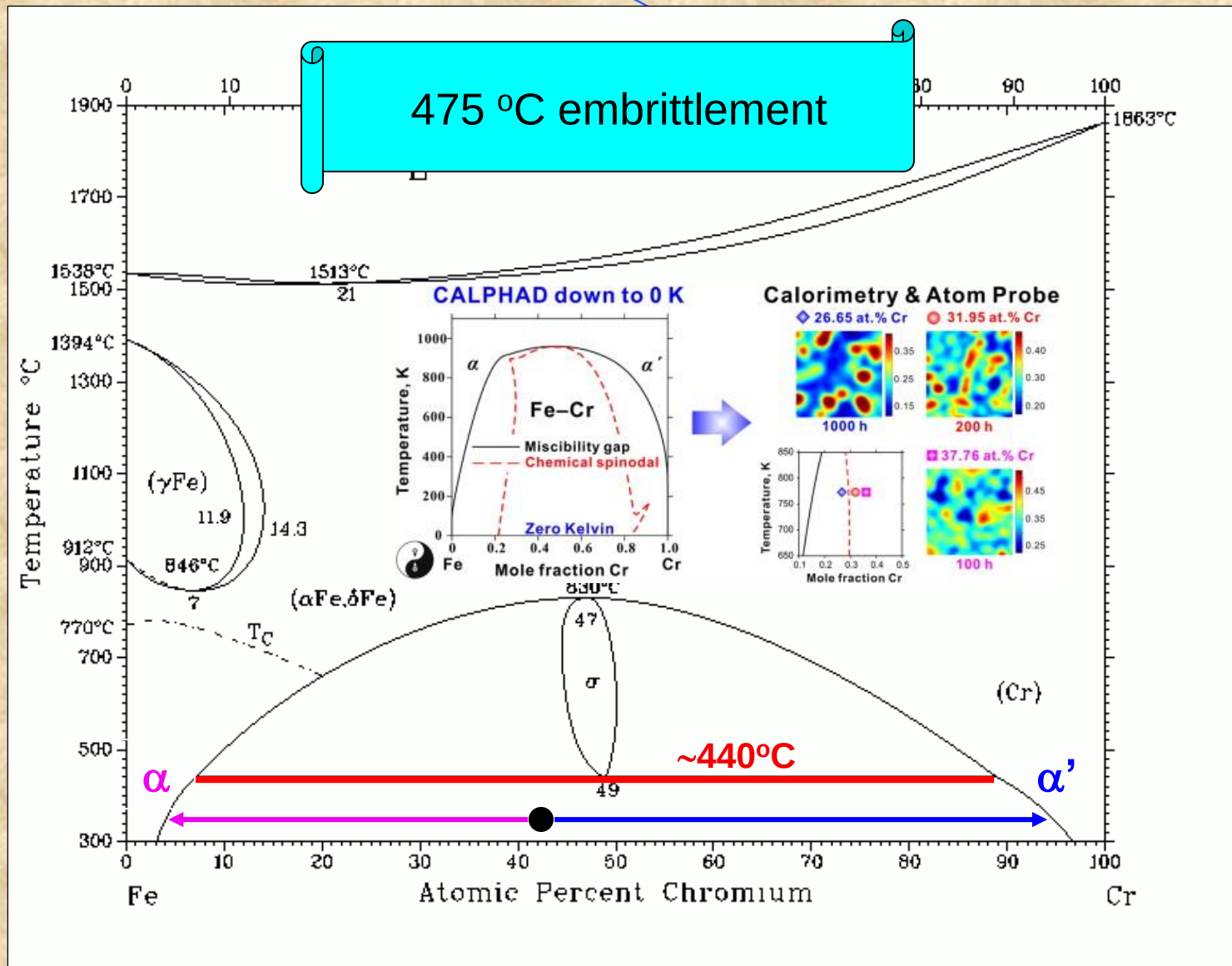


SRO in Fe-Cr - MS

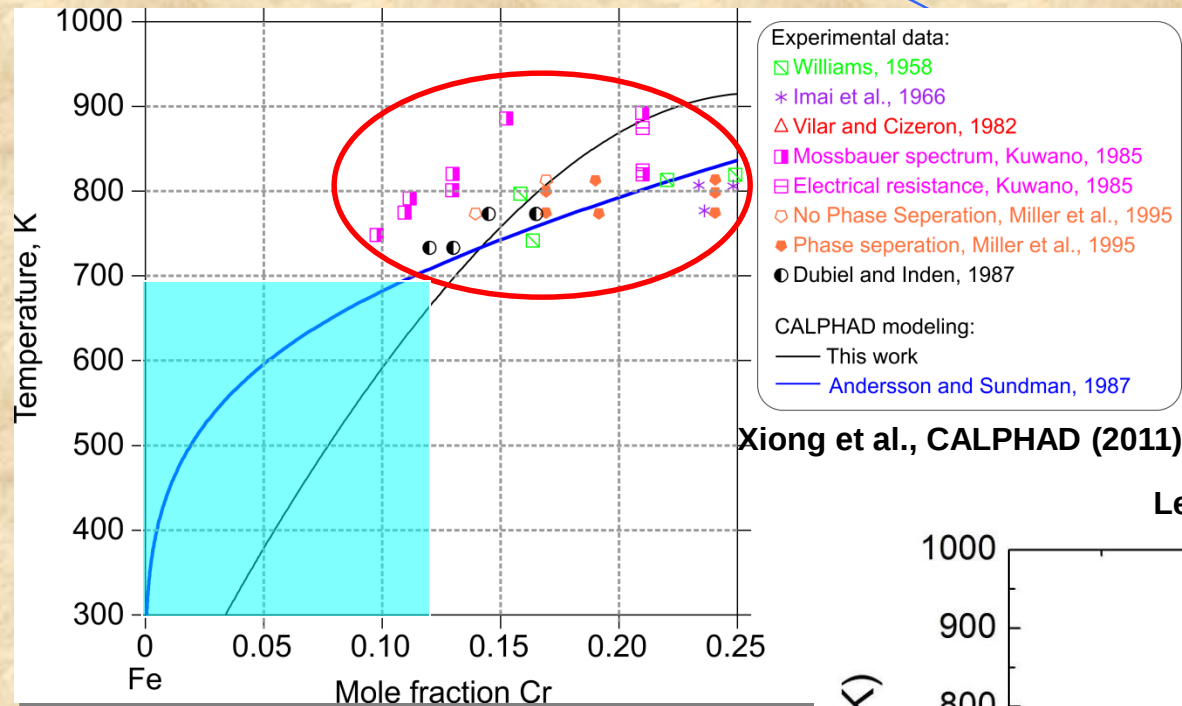


- ND
- I. Mirebeau, PRB (2010)
- MS (EQ)
- MS (Q)
- MS (CR)

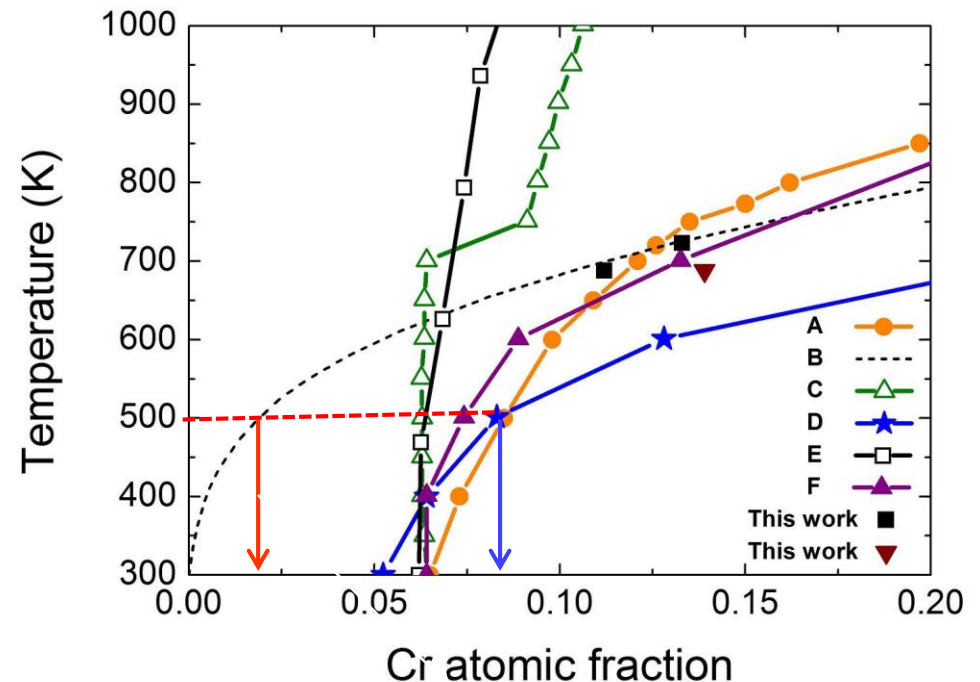
Phase decomposition into α and α'



Miscibility gap boundary

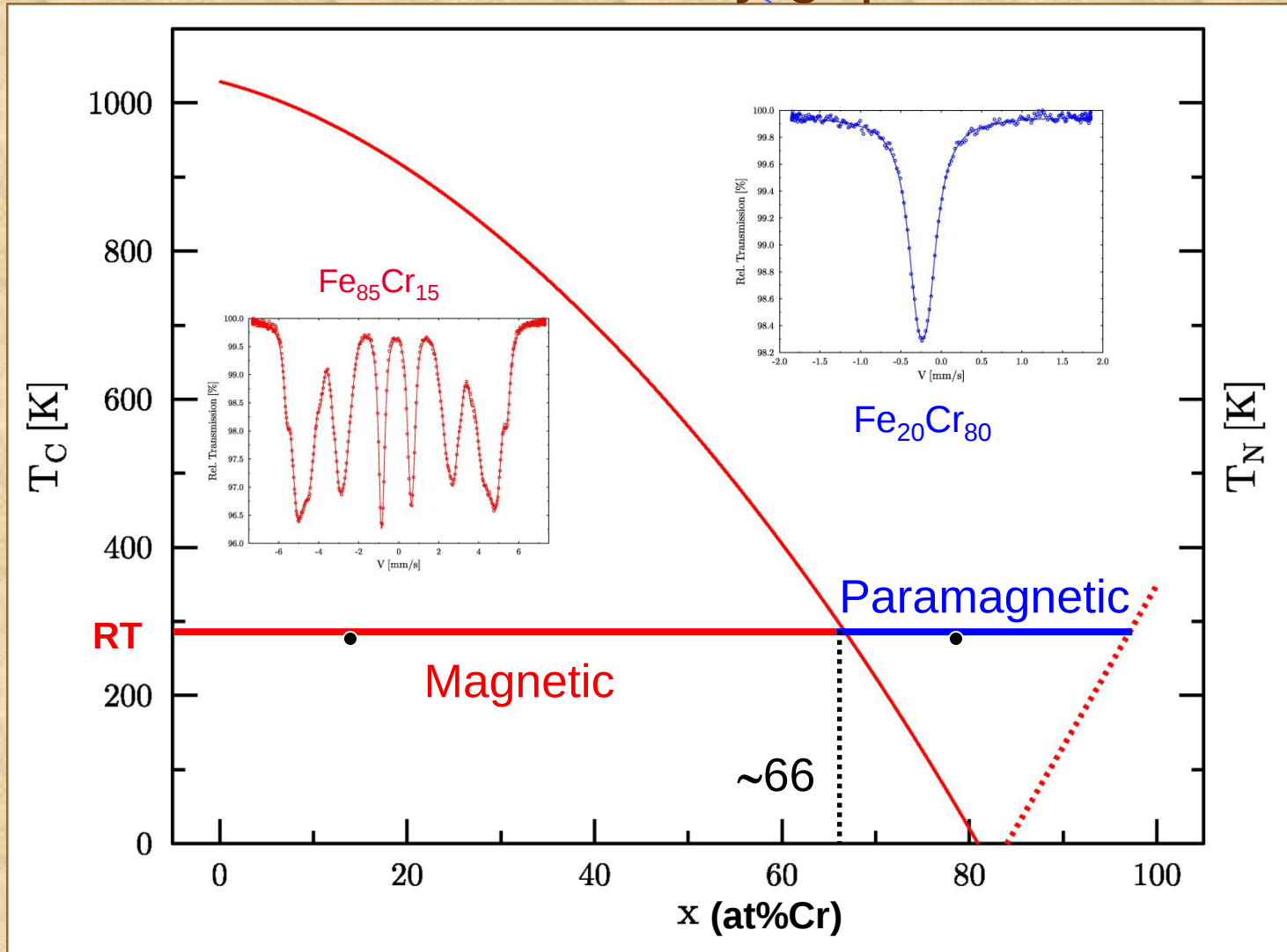


Levesque et al., PRB, 84 (2011) 184205



Phase decomposition into α and α'

- Borders of miscibility gap



Borders of miscibility gap

S. M. Dubiel & G. Inden, Z. Metallkde, 78 (1987) 544

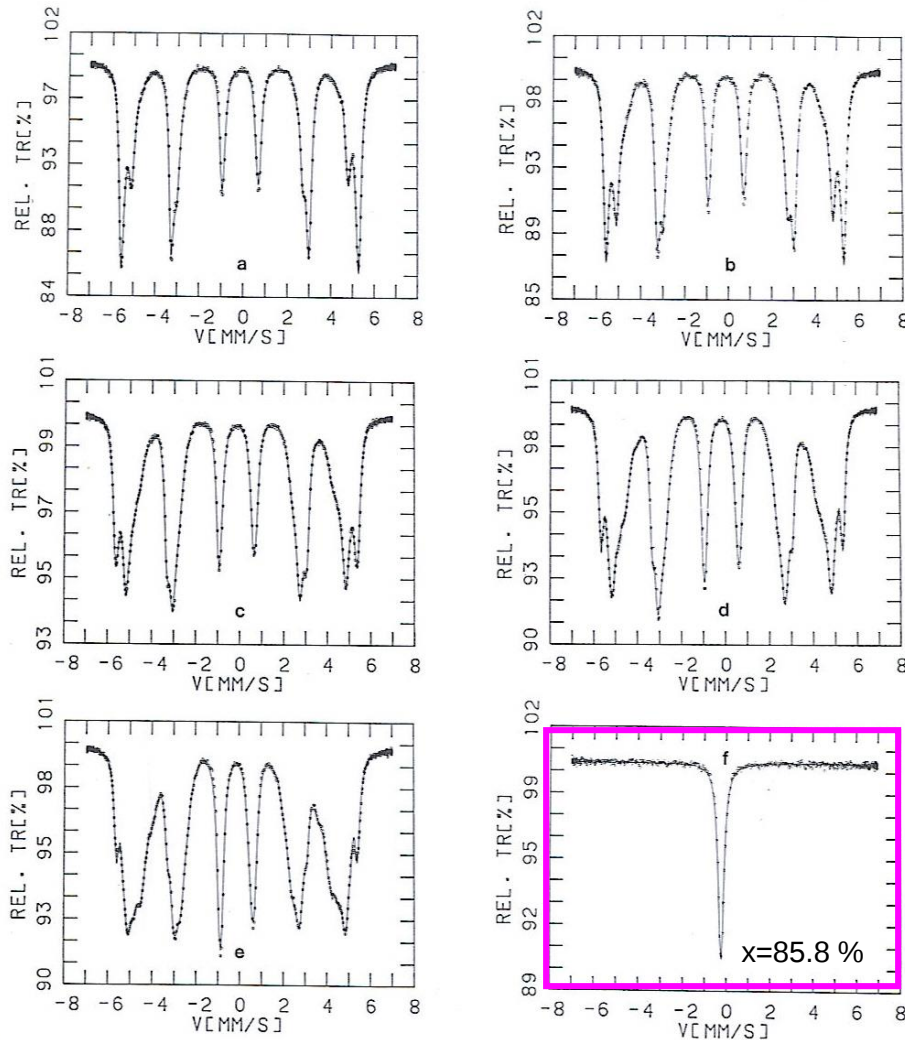
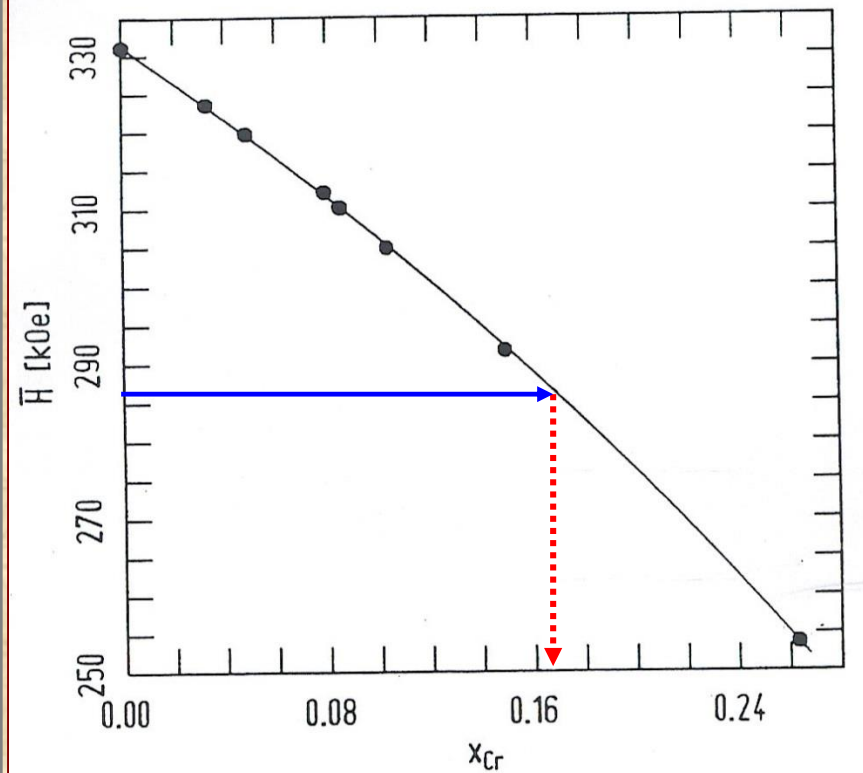


Fig. 3a to f. Room temperature Mössbauer spectra of single phase $\text{Fe}_{1-x}\text{Cr}_x$ alloys with (a) $x = 0.033$, (b) $x = 0.0485$, (c) $x = 0.079$, (d) $x = 0.103$, (e) $x = 0.149$, and (f) $x = 0.858$. The solid lines represent the fitted spectra.



Borders of miscibility gap

- Annealed samples: (a) 15, (b) 20.8, (d) 70.6 at%Cr

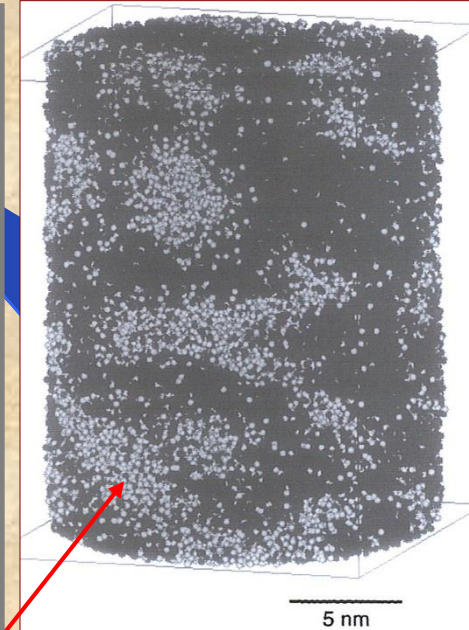
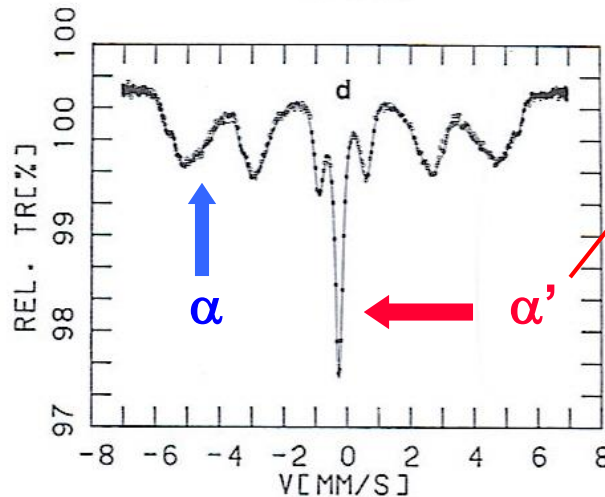
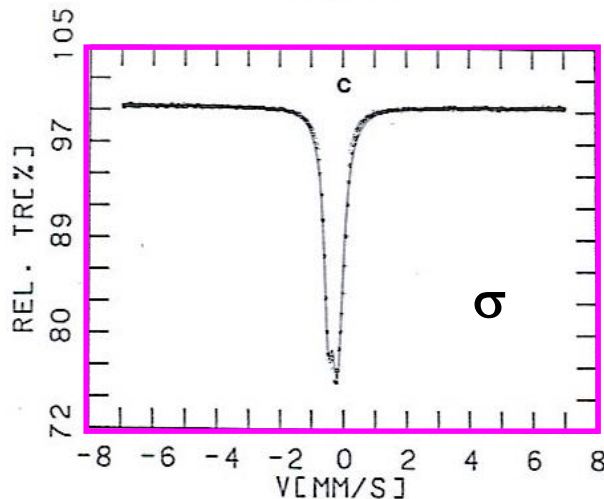
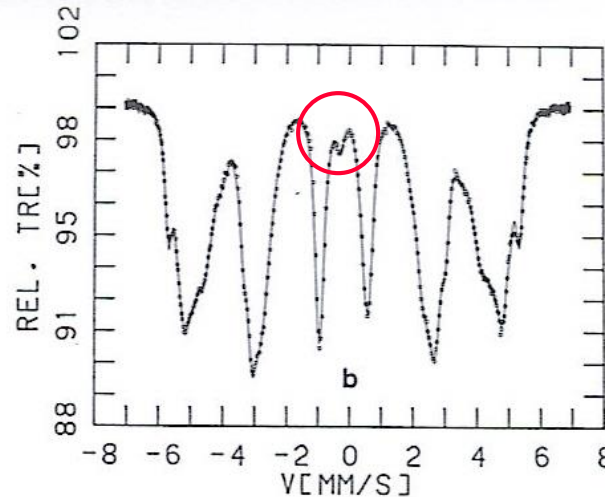
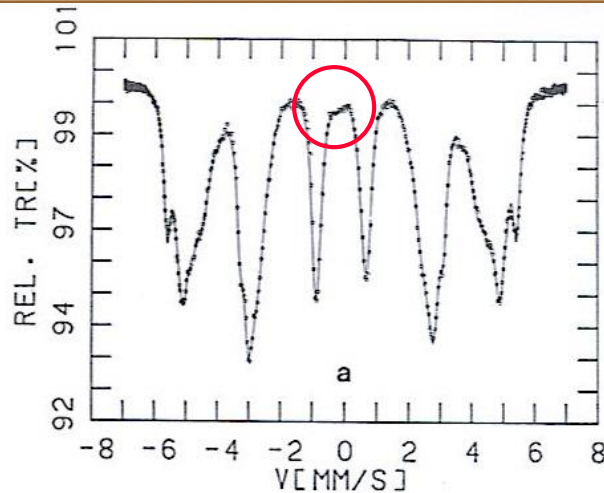
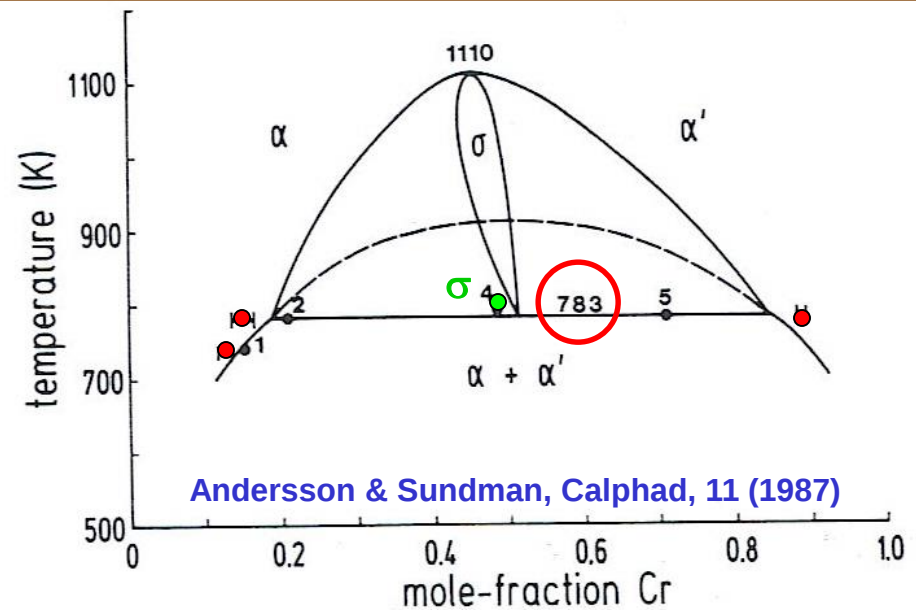
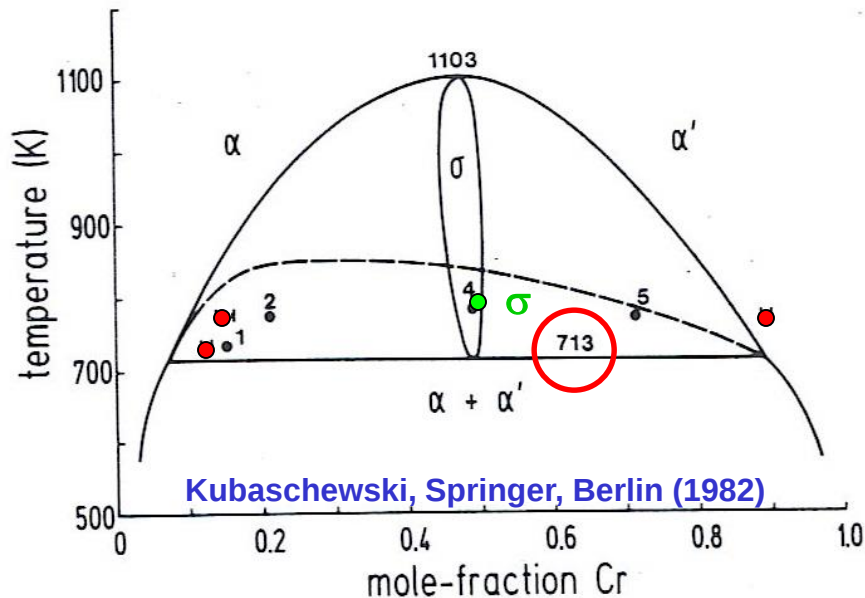


Fig. 8a to d. Room temperature Mössbauer spectra of the long term annealed alloys (a) no. 1, (b) 2, (c) 4, and (d) 5. The spectra (a), (b) and (d) correspond to two-phase states $\alpha + \alpha'$, spectrum (c) corresponds to the σ phase. The solid lines represent the fitted spectra.

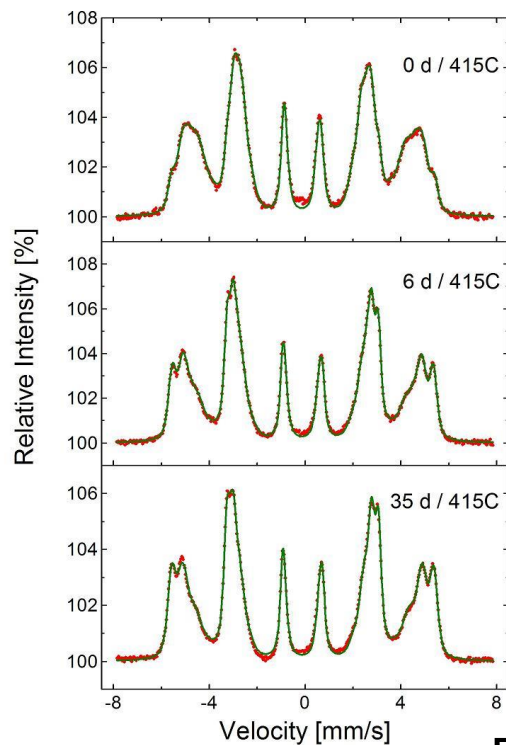
S. M. Dubiel & G. Inden,
Z. Metallkde, 78 (1987) 544

Borders of miscibility gap

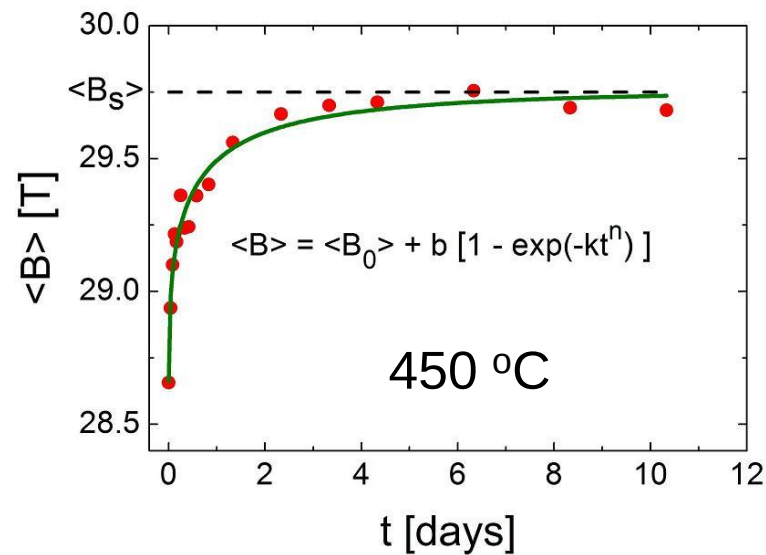
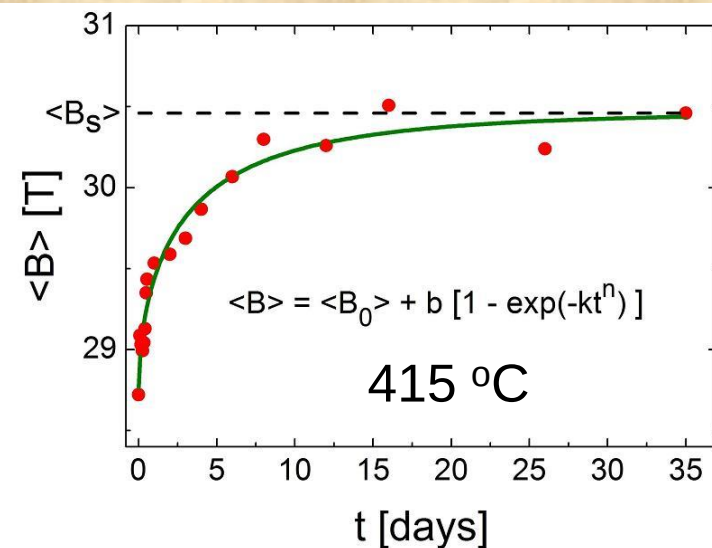
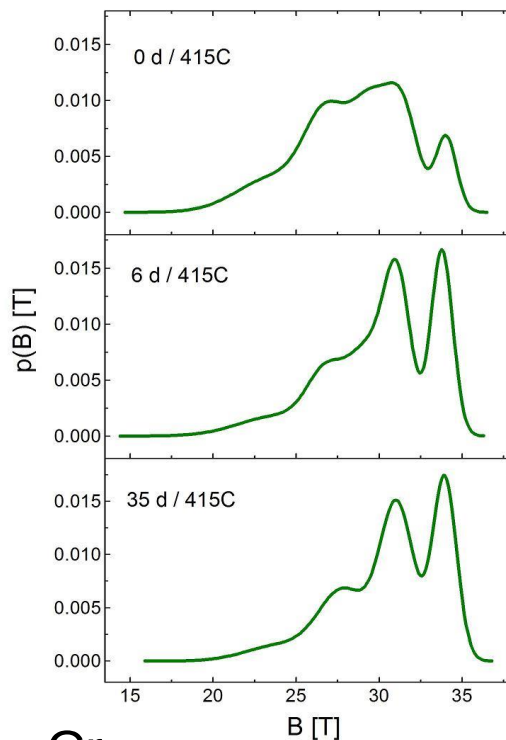
x (%)	$x_{\alpha}(<N>)$	$x_{\alpha}(<H>)$	$x_{\alpha'}$
15.0	12.9	12.0	-
20.8	14.3	14.0	-
70.6	15.7	16.5	88.0



Borders of miscibility gap

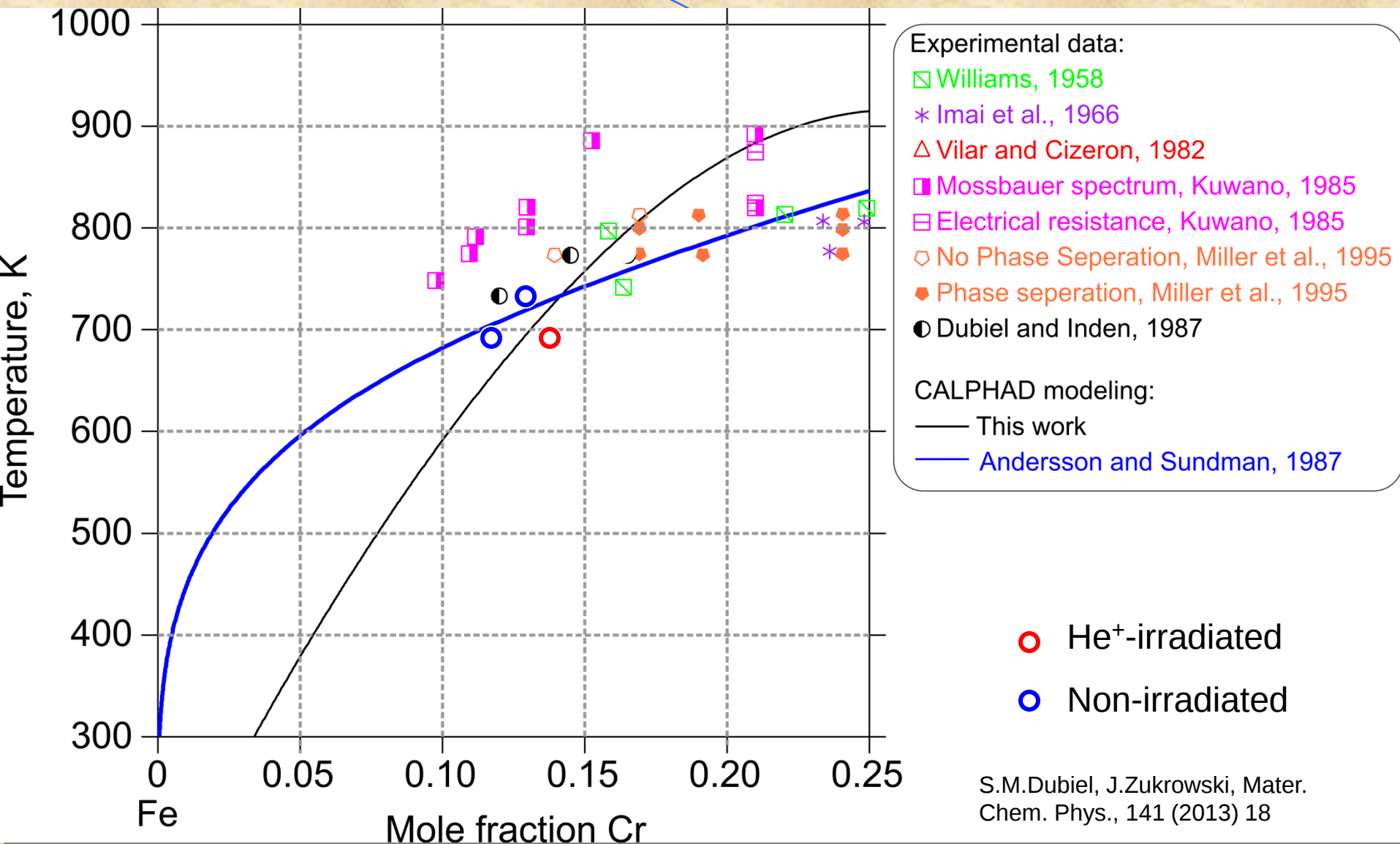


$\text{Fe}_{85}\text{Cr}_{15}$



T (°C)	Sample	x_{Cr} (%)
415	NR	11.2(3)
415	IR	13.9(3)
450	NR	13.3(3)

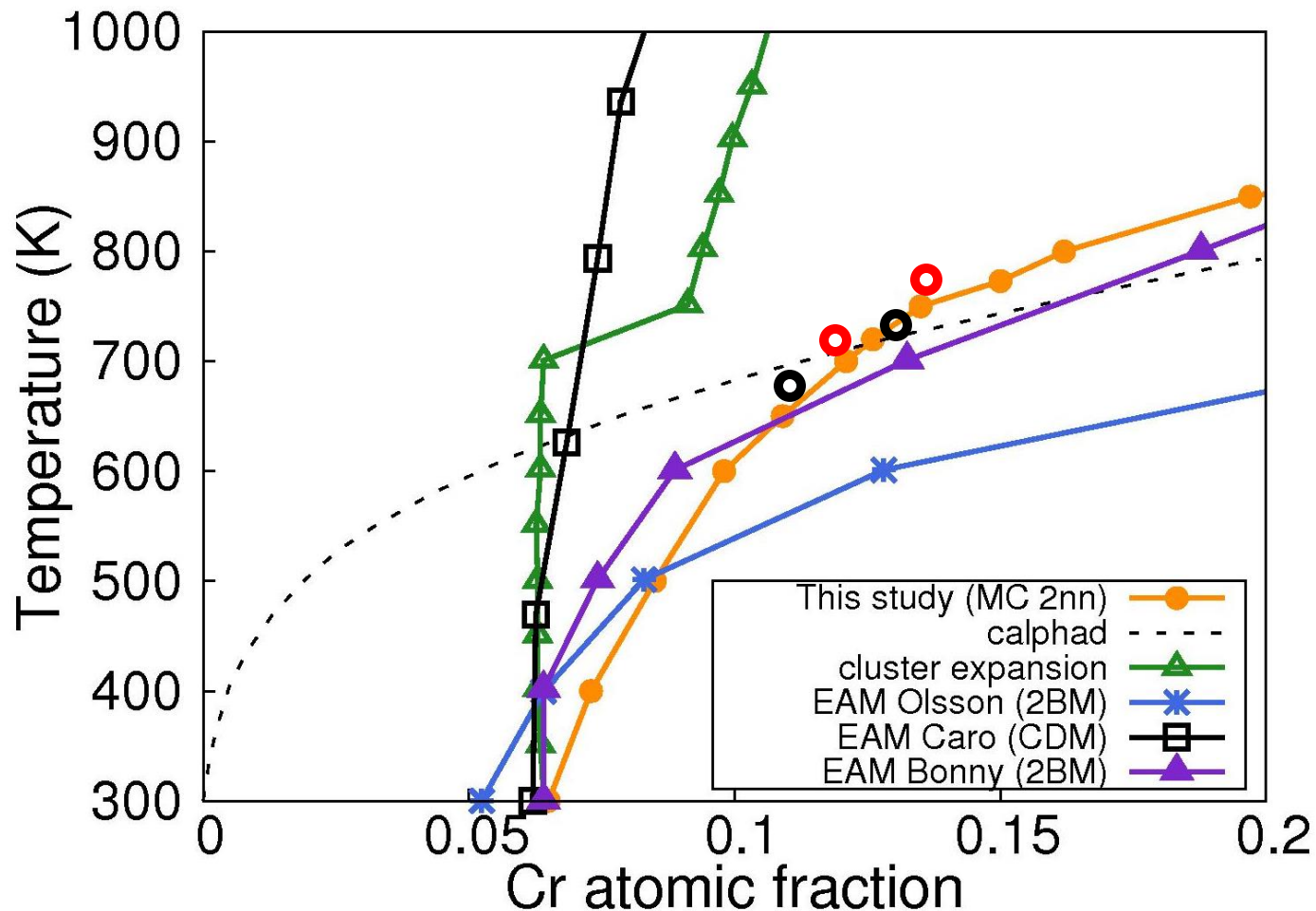
Borders of miscibility gap



S.M.Dubiel, J.Zukrowski, Mater.
Chem. Phys., 141 (2013) 18

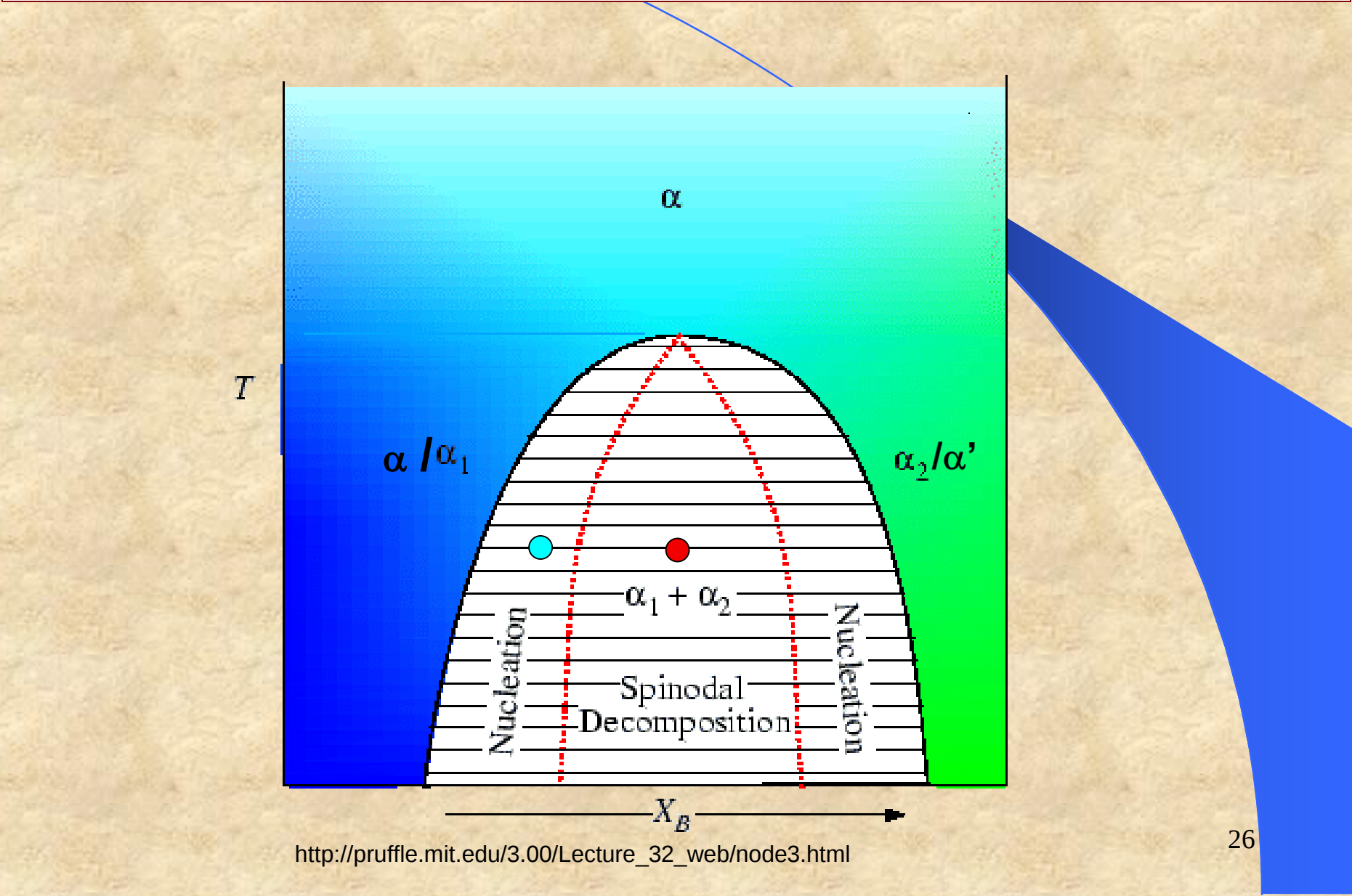
Borders of miscibility gap

M. Levesque *et al.*, PRB, 84 (2011) 184205



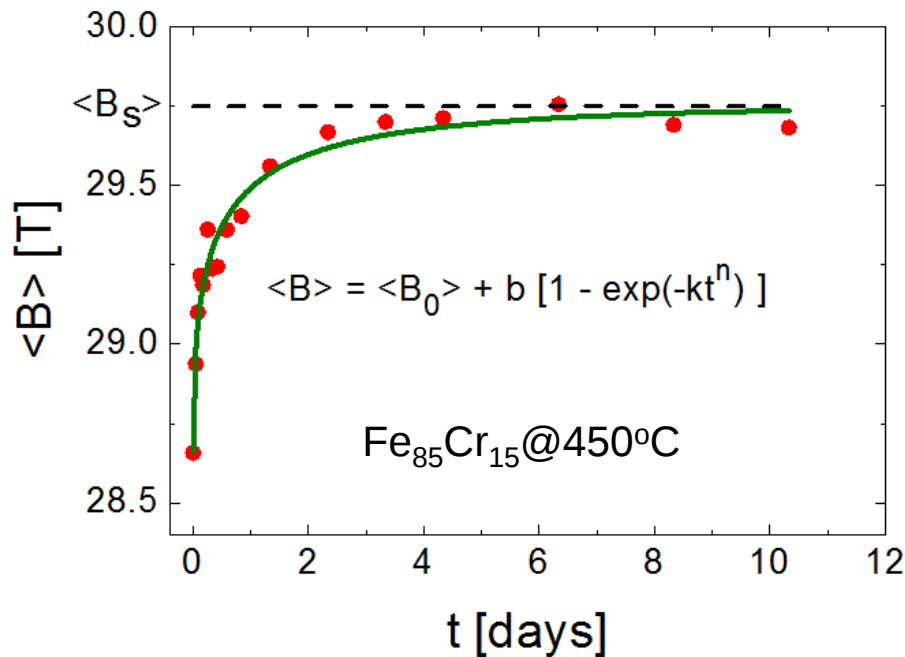
● Dubiel & Inden (1987); ● Dubiel & Zukrowski (2013)

26



Phase decomposition into α and α'

- Kinetics of decomposition



Arrhenius law

$$k = k_0 \exp\left(-\frac{E}{k_B T}\right)$$

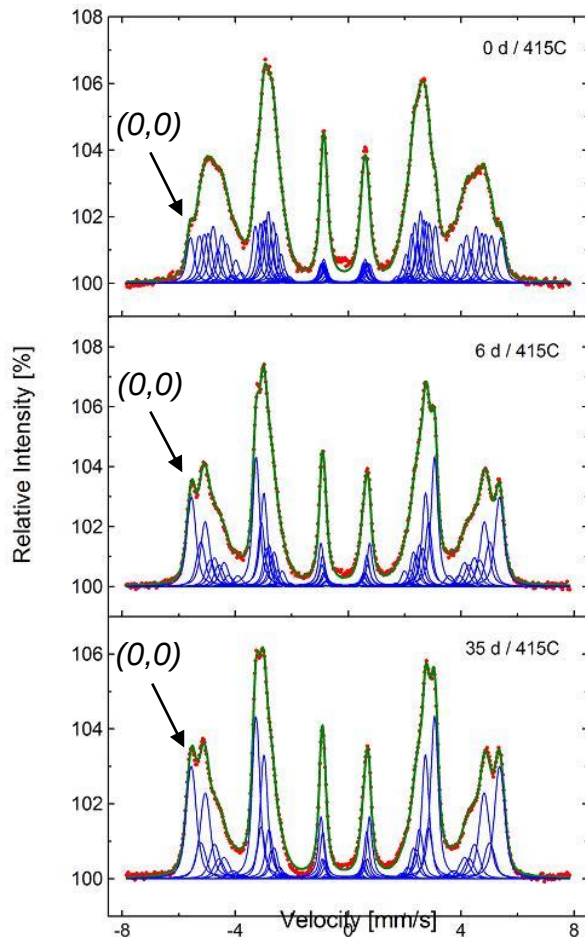
$$E = \frac{T_1 T_2}{T_2 - T_1} k_B \ln\left(\frac{k_2}{k_1}\right)$$

122 kJ/mol

T (°C)	Sample	x_{Cr} (%)	n	k [s ⁻¹]
415	NR	11.2(3)	0.6(1)	0.3
415	IR	13.9(3)	1.0(3)	3.9
450	NR	13.3(3)	0.4(5)	2.2

Phase decomposition into α and α'

- Short-range ordering: $\text{Fe}_{85}\text{Cr}_{15}$ @ 415°C



- Each spectrum was analyzed in terms of 17 subspectra (sextets) corresponding to particular atomic configurations (m, n)

- Analysis yielded probabilities of (m, n), $P(m, n)$, based on which the average number of Cr atoms in 1NN, $\langle m \rangle$, that in 2NN, $\langle n \rangle$, and the one in 1NN-2NN, $\langle m+n \rangle$, was determined.

- SRO parameters, α_1 , α_2 , α_{12} , were next calculated from the following equations:

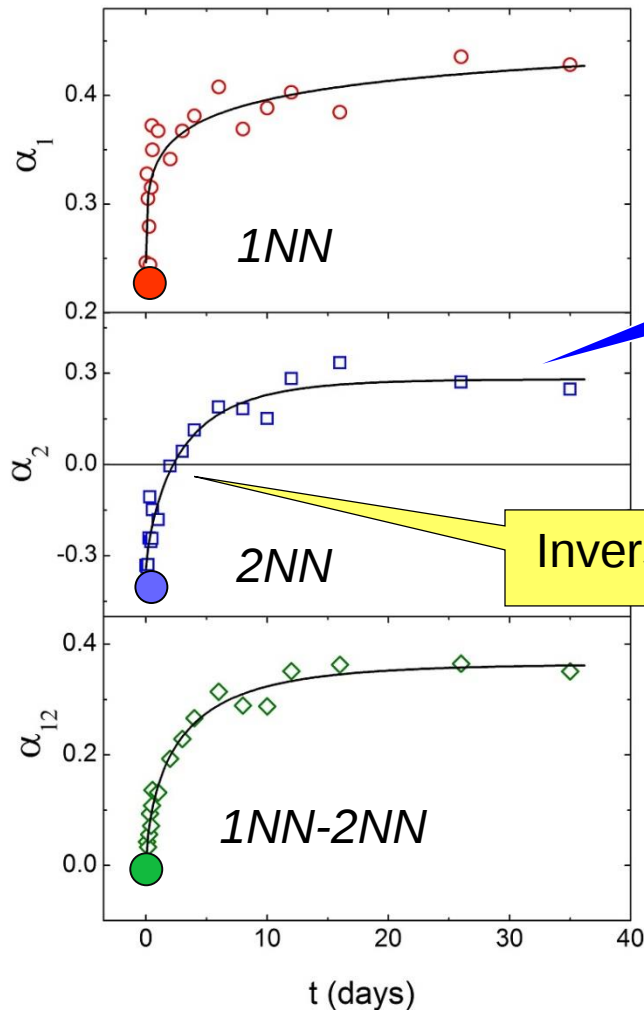
$$\alpha_1 = 1 - \frac{\langle m \rangle}{8x}$$

$$\alpha_2 = 1 - \frac{\langle n \rangle}{6x}$$

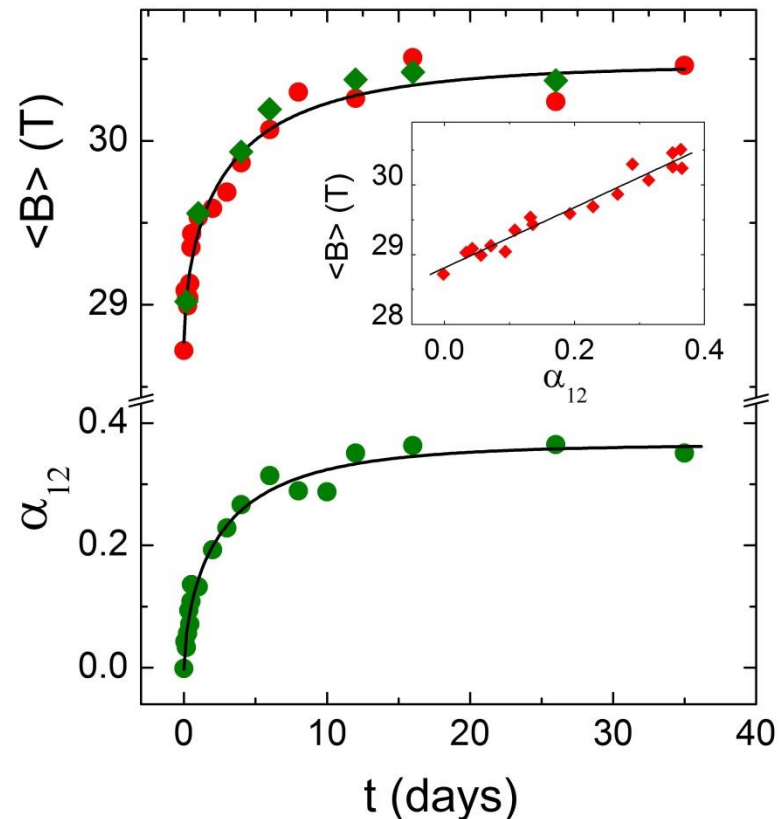
$$\alpha_{12} = 1 - \frac{\langle m+n \rangle}{14x}$$

Phase decomposition into α and α'

- Short-range ordering: $\text{Fe}_{85}\text{Cr}_{15}$ @ 415°C



Solid lines represent best fits in terms of JMAK-like equation, hence α_{12} is linearly correlated with $\langle B \rangle$.

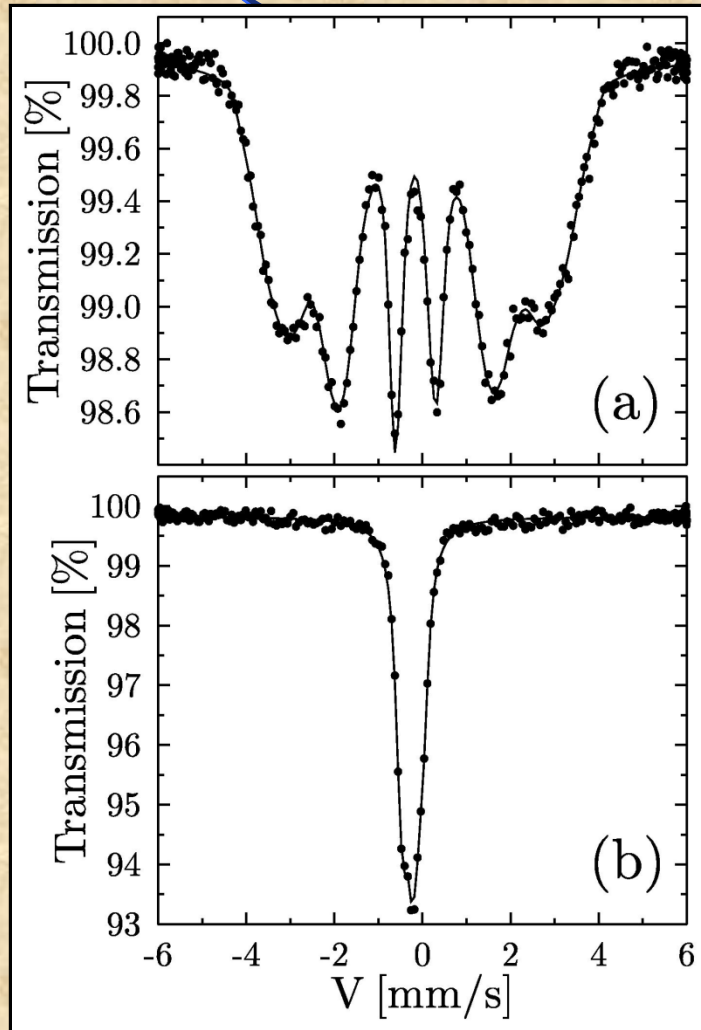
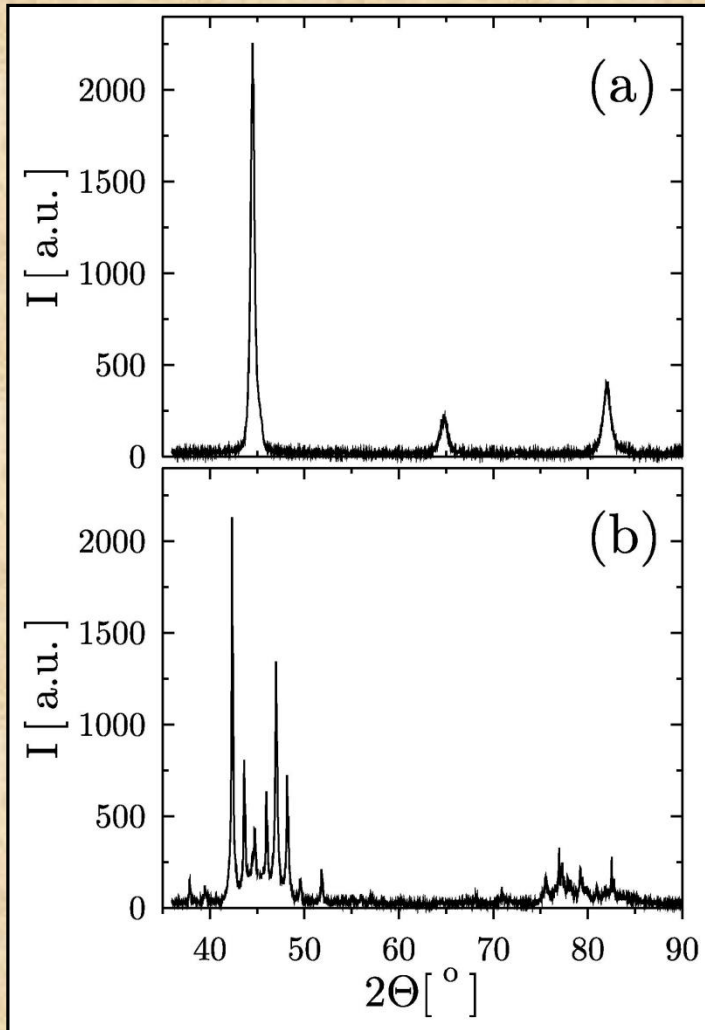


Sigma (σ) phase - identification

XRD

• T = 295 K

MS



σ phase - kinetics

$$T_a = 700^\circ\text{C}$$

$$A_\sigma = \frac{S_\sigma}{S_\sigma + S_\alpha} 100$$

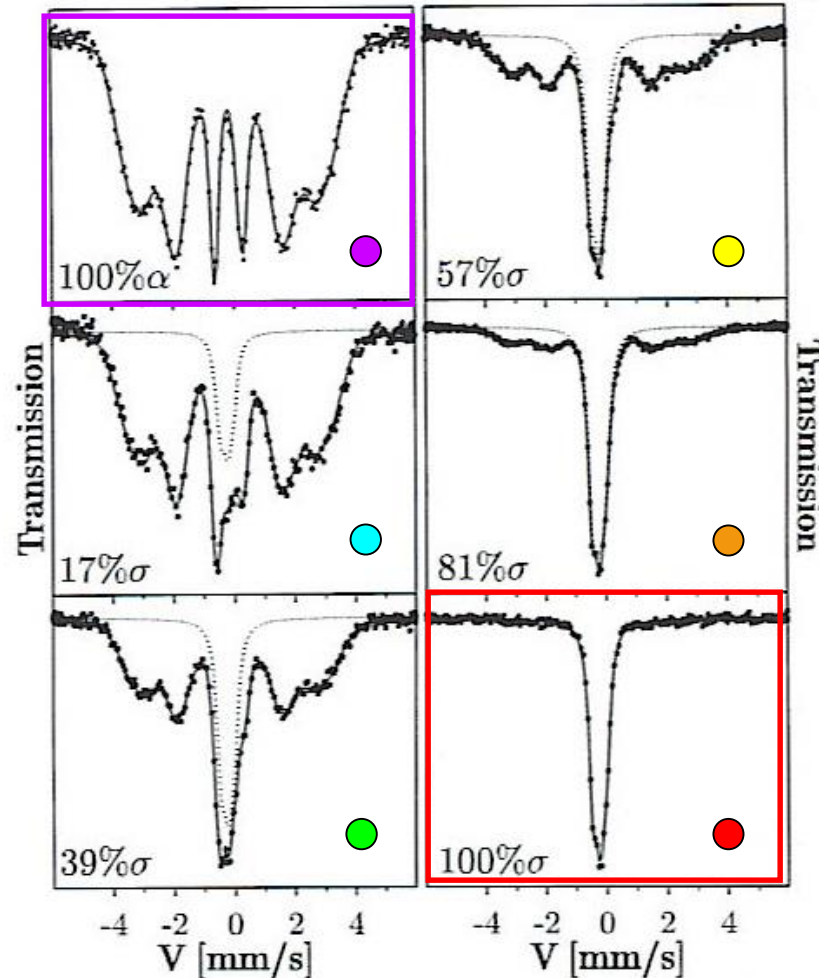
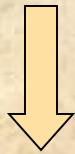


Fig. 1. Room temperature ^{57}Fe Mössbauer spectra recorded on an $\text{Fe}_{53.8}\text{Cr}_{46.2}\text{Ti}$ sample with various amounts of the σ -phase formed. Its subspectrum has been marked by a dotted line.

Sigma (σ) phase - kinetics

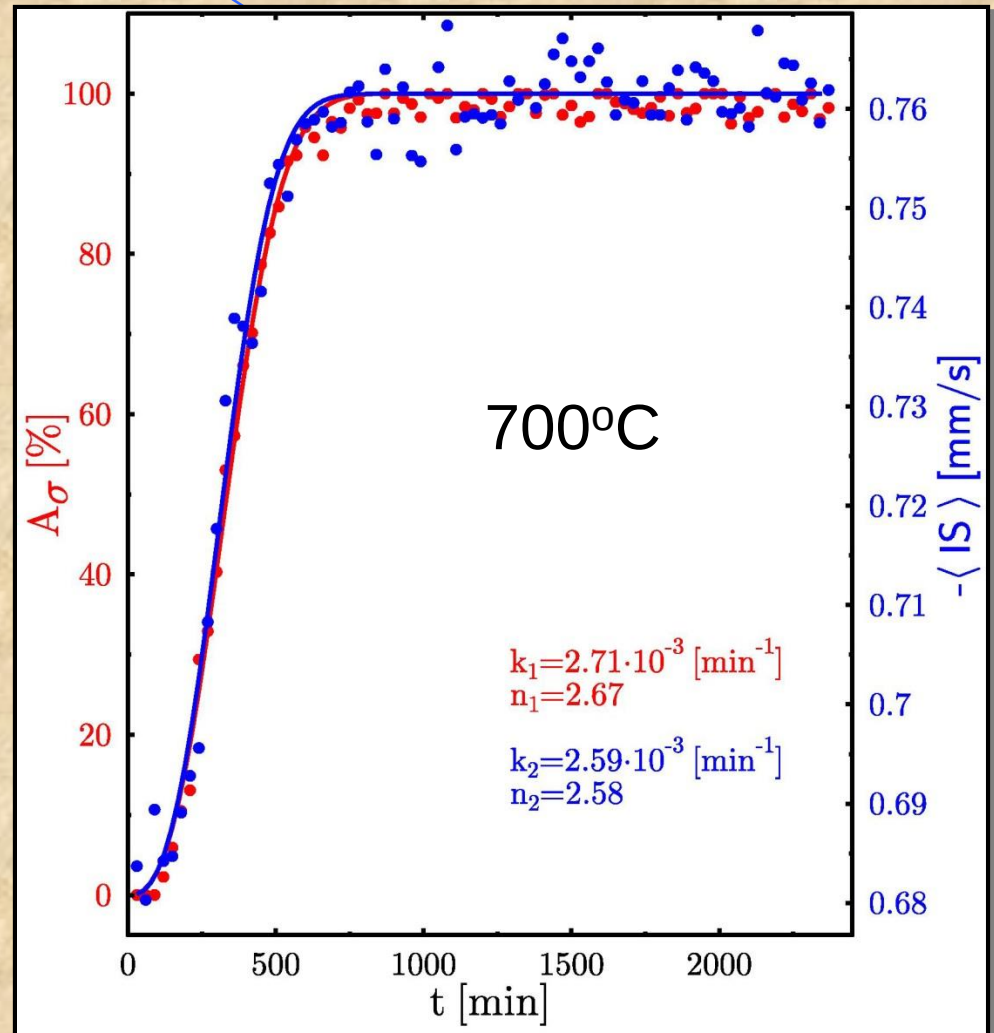
$$A_{\sigma} = 100[1 - \exp[-kt^n]]$$



$$k = k_o \exp\left(-\frac{E}{RT}\right)$$

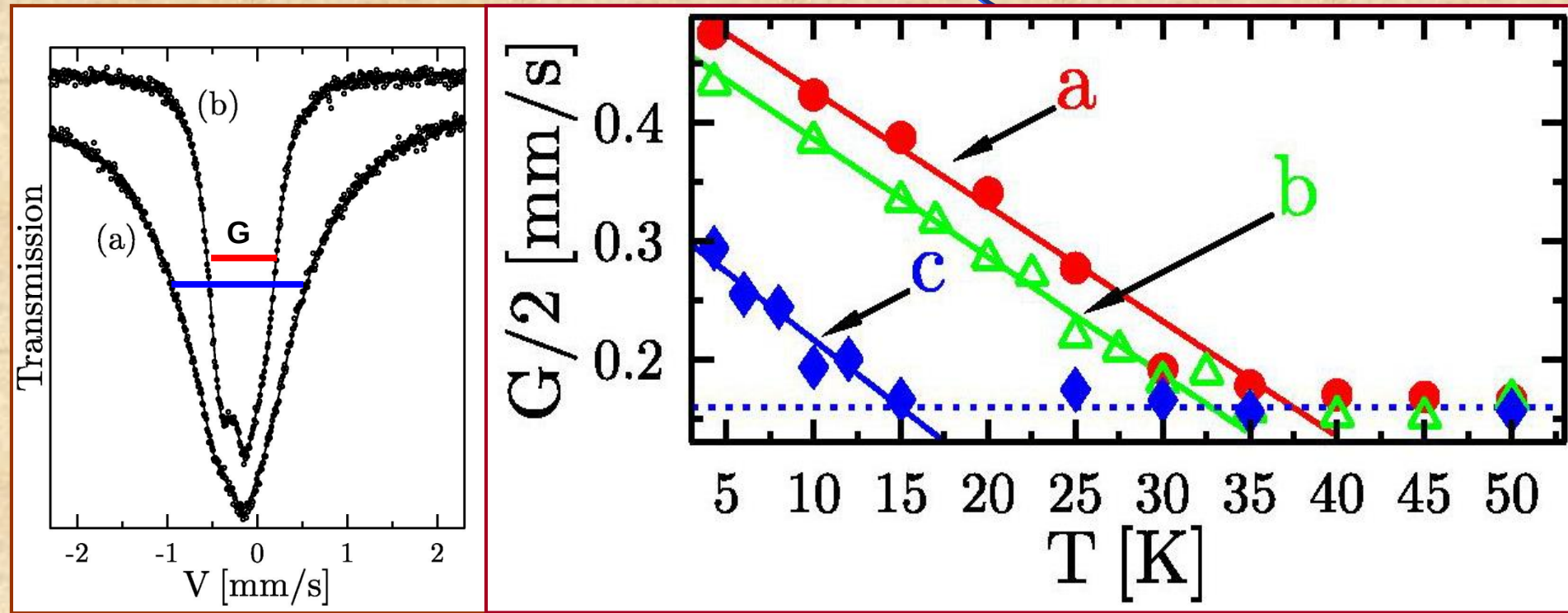


$$E = 196 \pm 2 \text{ kJ/mol}$$



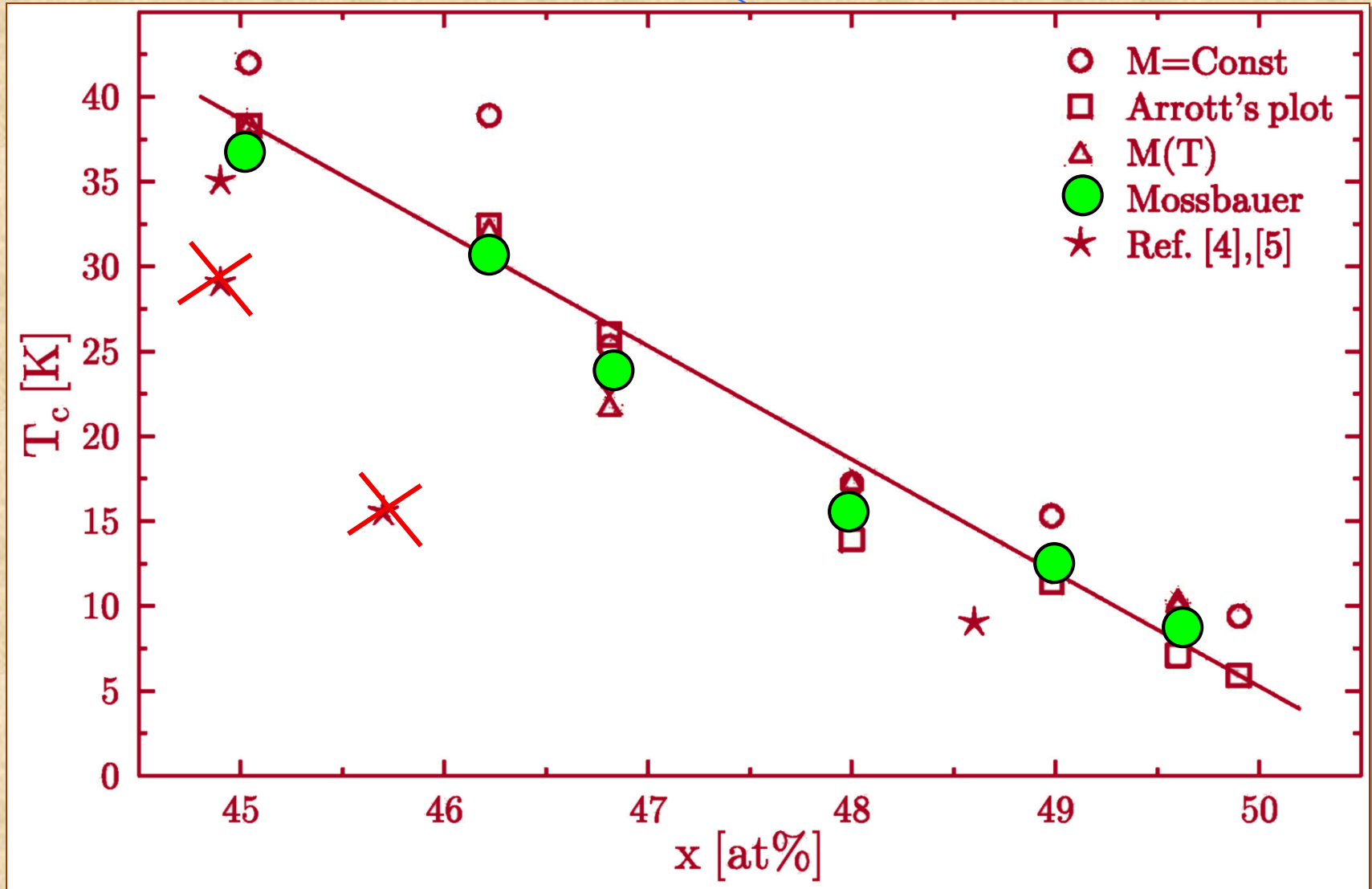
σ phase – Curie Temperature

(a) 4.2 K; (b) 295 K



(a) $x = 45.0$ (b) $x = 46.2$ and (c) $x = 48.0$

σ – Curie Temperature

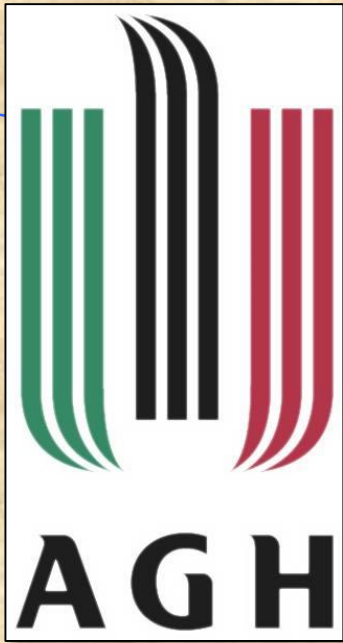


Summary

Mössbauer Spectroscopy is a very useful techniques to quantitatively investiagte various issues pertinent to Fe-Cr alloys, and in particular:

- Short-rane ordering
- Borders of misceptibility gap
- Kinetics of phase separation
- Sigma-phase identification and its kinetics
- Magnetic ordering temperatures

Acknowledgements





Thank you for
listening!

Mössbauer Effect

Radiation	E [keV]	Intensity	Range* [nm]
γ	14.4	0.11	~20 000
X-K	6.3	0.28	~20 000
X-L	0.7	0.002	
CE-K	7.3	0.79	~10-400
CE-L	13.6	0.08	~20-1 300

* In metallic Fe

Range for He (25 keV) ~225 nm